



# BUSINESS INCOME UNDERREPORTING AND PUBLIC FINANCE

A. BHANDARI, E. MCGRATTAN, Y. YAO

FEBRUARY 2024



# The Macroeconomics of US Public Finance

- Net government saving  $\approx -1$  \$Trillion (in 2018)
  - Current receipts: 5.6T
  - Current expenditures: 6.7T



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  - Current receipts: 5.6T
  - Current expenditures: 6.7T
- Untaxed business income  $\approx 1$  \$Trillion
  - Income reported to IRS: 3.2T
  - Estimate of true: 4.2T



# The Macroeconomics of US Public Finance

- Net government saving  $\approx -1$  \$Trillion
  - Current receipts: 5.6T
  - Current expenditures: 6.7T
- Untaxed pass-through income  $\approx 700$  \$Billion
  - Income reported to IRS: 1.3T
  - Estimate of true: 2T



# The Macroeconomics of US Public Finance

- Net government saving  $\approx -5.4\%$  GDP
  - Current receipts: 27%
  - Current expenditures: 33%
- Untaxed pass-through income  $\approx 3.4\%$  GDP
  - Income reported to IRS: 6.4%
  - Estimate of true: 9.8%



# The Macroeconomics of US Public Finance

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  - Current expenditures: 33%
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  - Estimate of true: 9.8%

$\Rightarrow$  Prompting more funding for IRS enforcement



# Greater IRS Enforcement

- Inflation Reduction Act:
  - 80 billion over 10 years
  - Enforcement budget roughly doubled
- Predicted returns on investment (ROI):
  - CBO/JCT (2021): 5–9%
  - Boning et al (2023): 5–12%



## This Paper

- First step before using IRS micro data
  - Use public IRS compliance data (TCMP/NRP)
  - Develop dynamic GE model of tax evasion
  - Compare higher tax vs enforcement counterfactuals
- Useful for next steps
  - Data: expand collection to business filings
  - Theory: add transition dynamics and welfare analysis





## What's New?

- Factors relevant for *dynamics of tax evasion*
    - Loss of *sweat capital* (eg, reputation, brands, etc)
    - Recovery of *back taxes*
  - Why relevant?
    - Impacts business dynamics and productivity
    - Amplifies precautionary motives
- ⇒ Economies with higher tax vs enforcement different



# IRS Compliance Data



## IRS Compliance Data

- Tax gap = random audits + DCE adjustments
- Random audits:
  - Taxpayer compliance measurement program, 1962–88
  - National research program, 2000–present
- *Detection controlled estimation* (DCE) adjustments:
  - Scale up recommendations of all examiners
  - Use data from examiners with largest adjustments



# How Big is the Tax Gap?

Gross tax gap	2001	2011	2021
Amount:			
billions of 2023\$	567	575	763
% of GDP	3.3	2.7	2.9

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## What is the Main Source of the Gap?

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Amount:			
billions of 2023\$	567	575	763
% of GDP	3.3	2.7	2.9
Source share:			
Underreporting	83	80	80
Underpayment	10	12	10
Nonfiling	7	8	11



# What is the Main Source of Underreporting?

Source share	2001	2011	2021
<b>Business</b>	62	55	55
Wages & salaries	4	3	2
Other	34	42	43



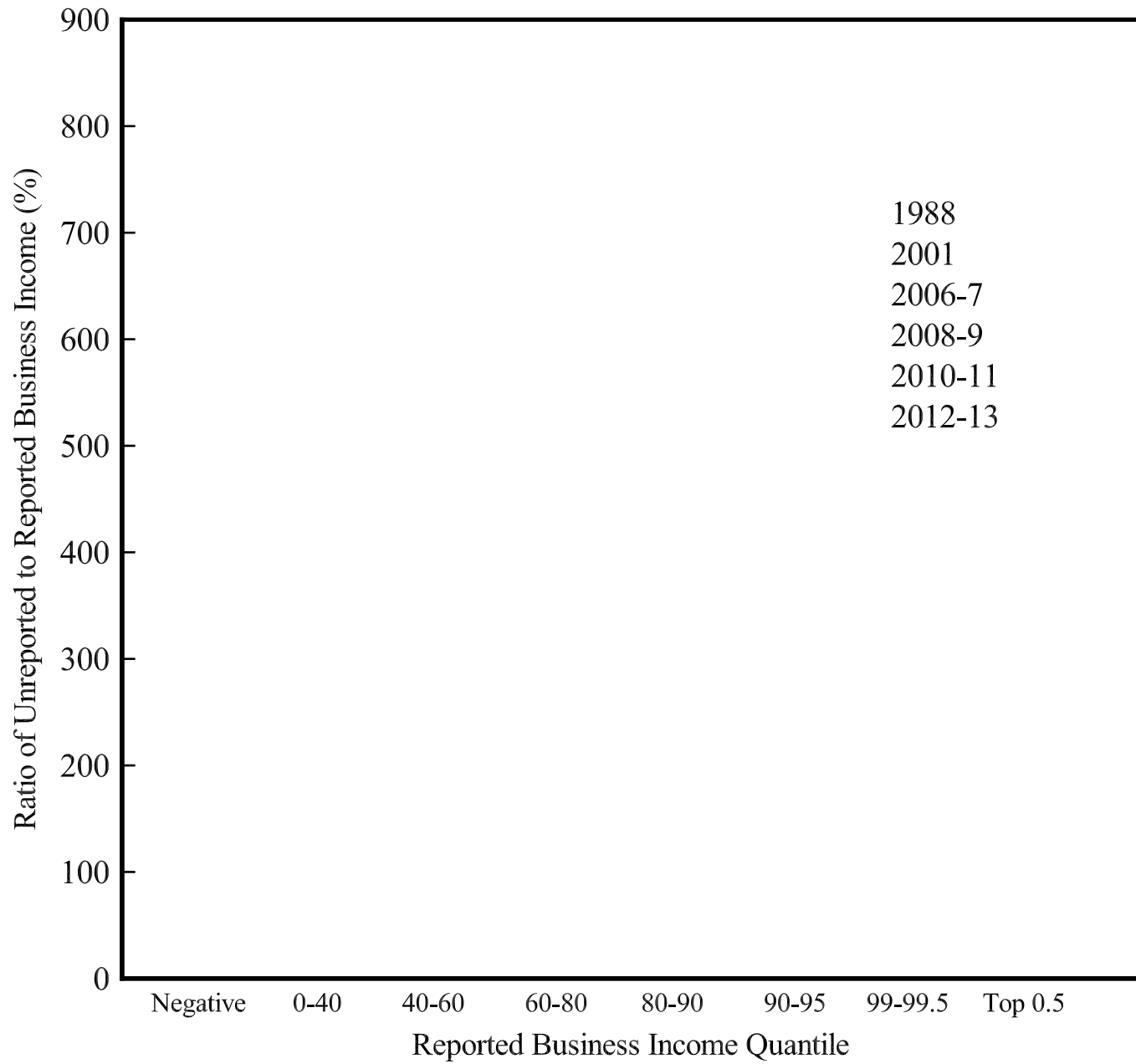
## How Widespread is Cheating?

- Evidence from NRP random-audit studies (no DCE)
  - All owners—ranked by reported incomes
  - Sole proprietors—ranked by understated tax
- Reveal same patterns
  - Cheating is widespread
  - Few owners account for most cheating



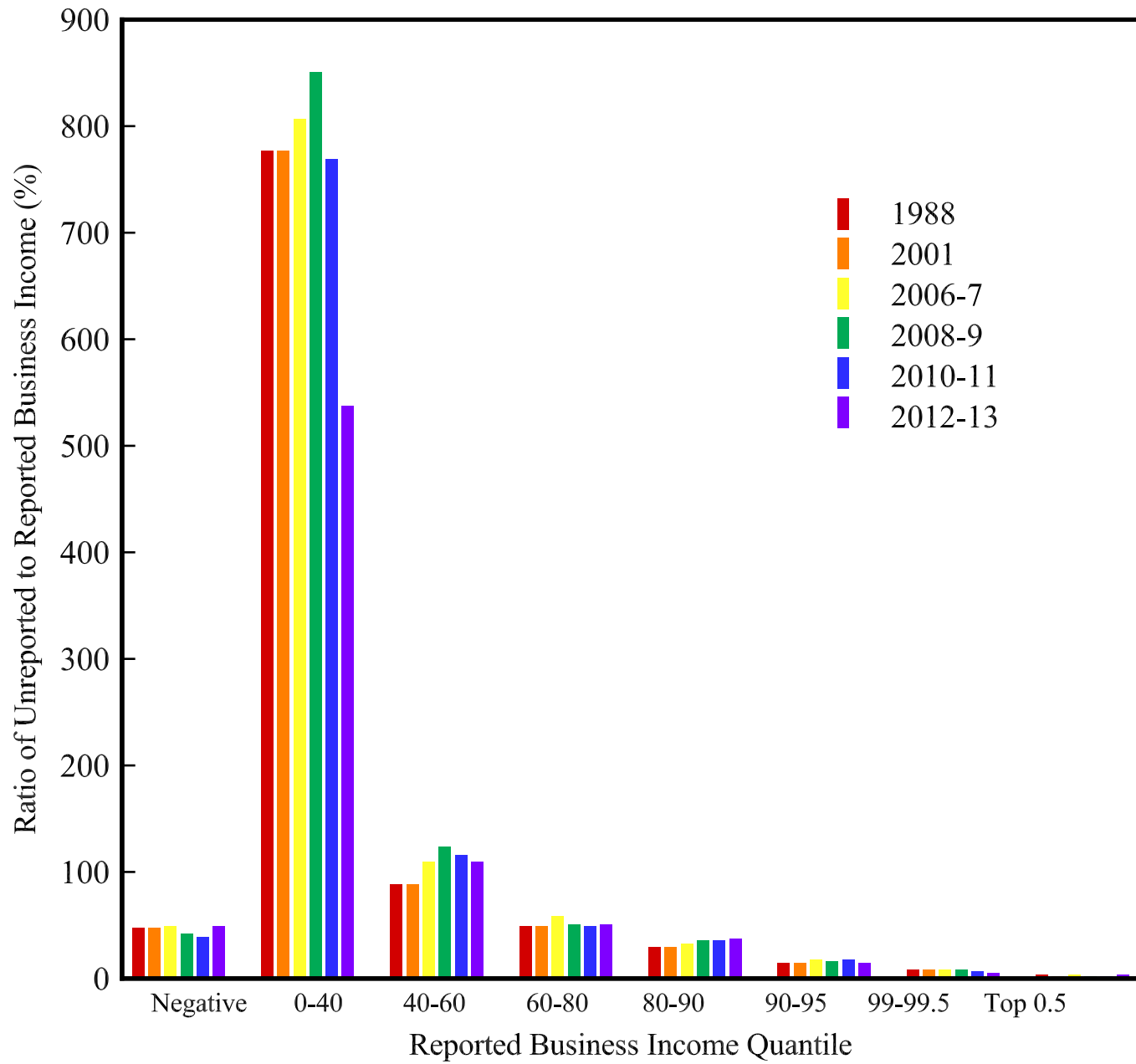


# Owners Ranked by Reported Incomes



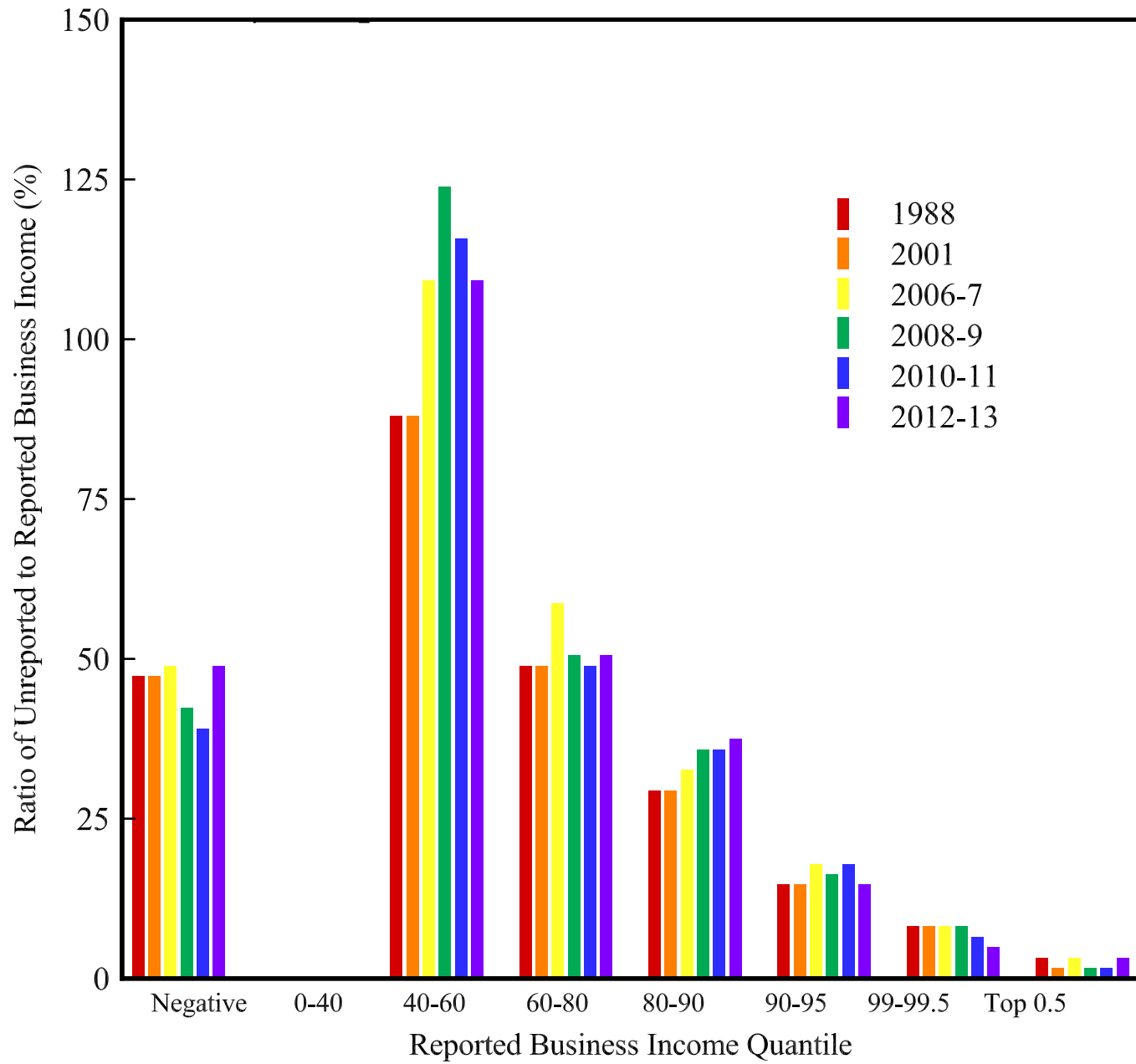


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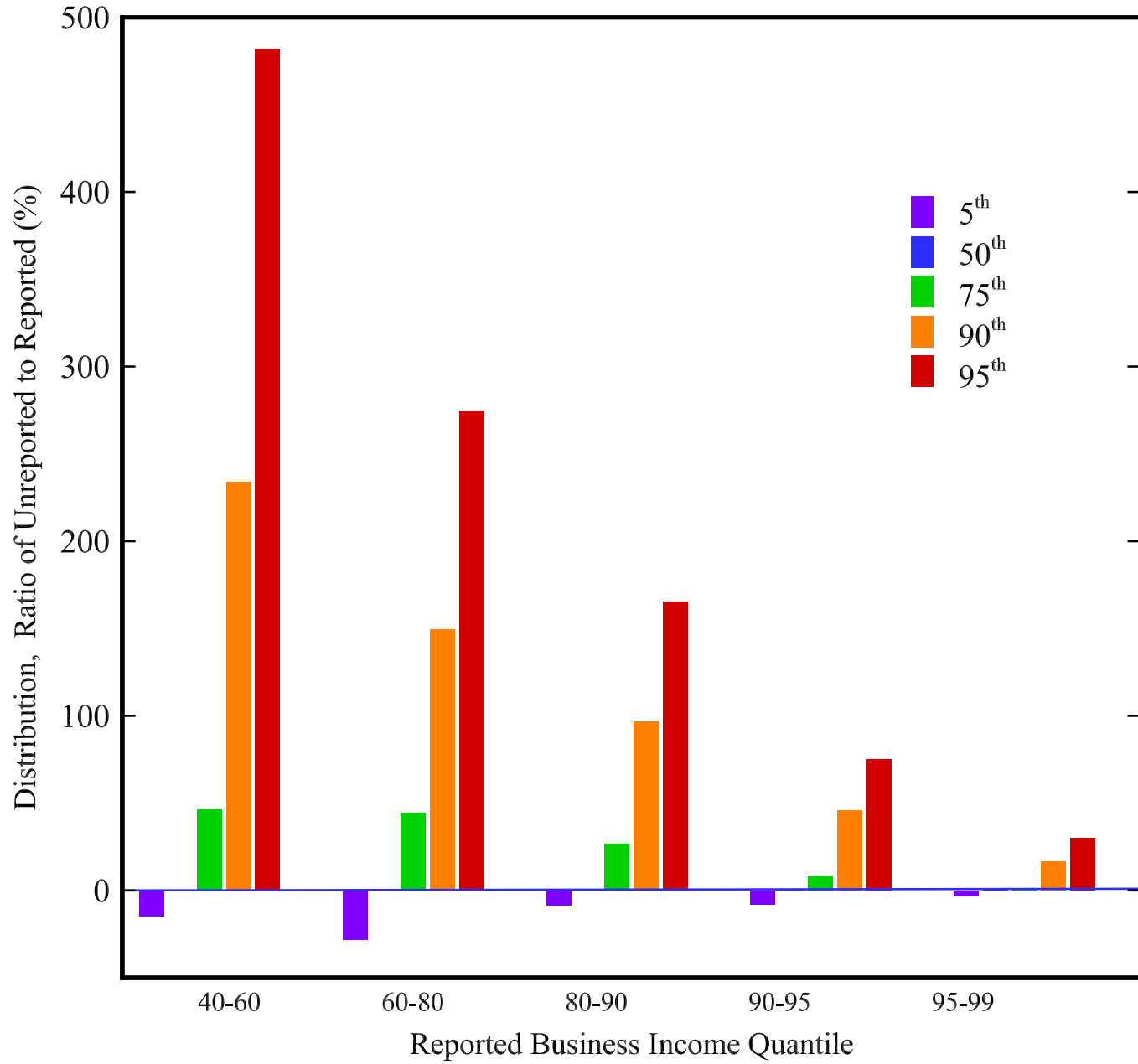


# Owners Ranked by Reported Incomes



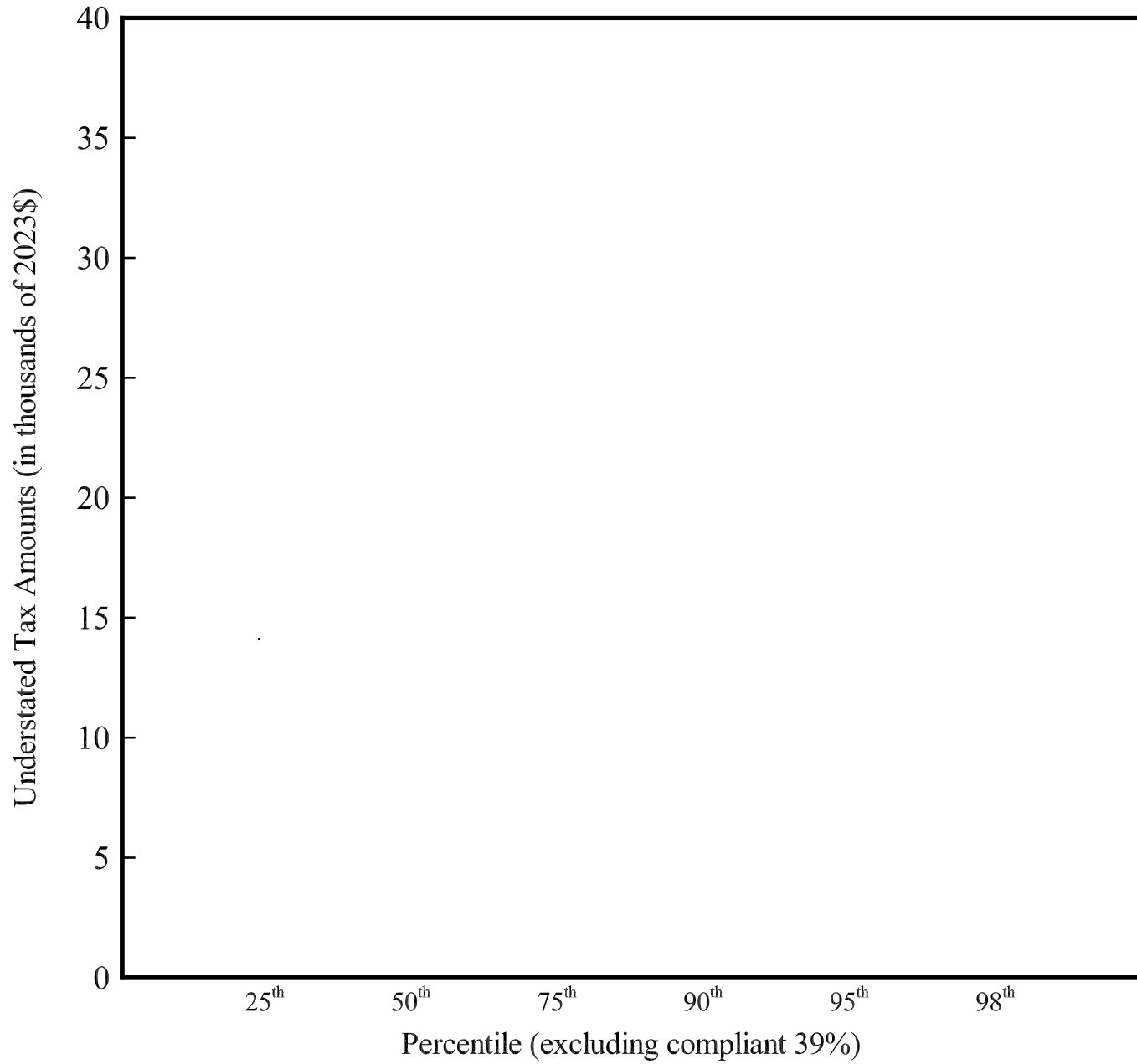


# Distribution of U-to-R Ratios



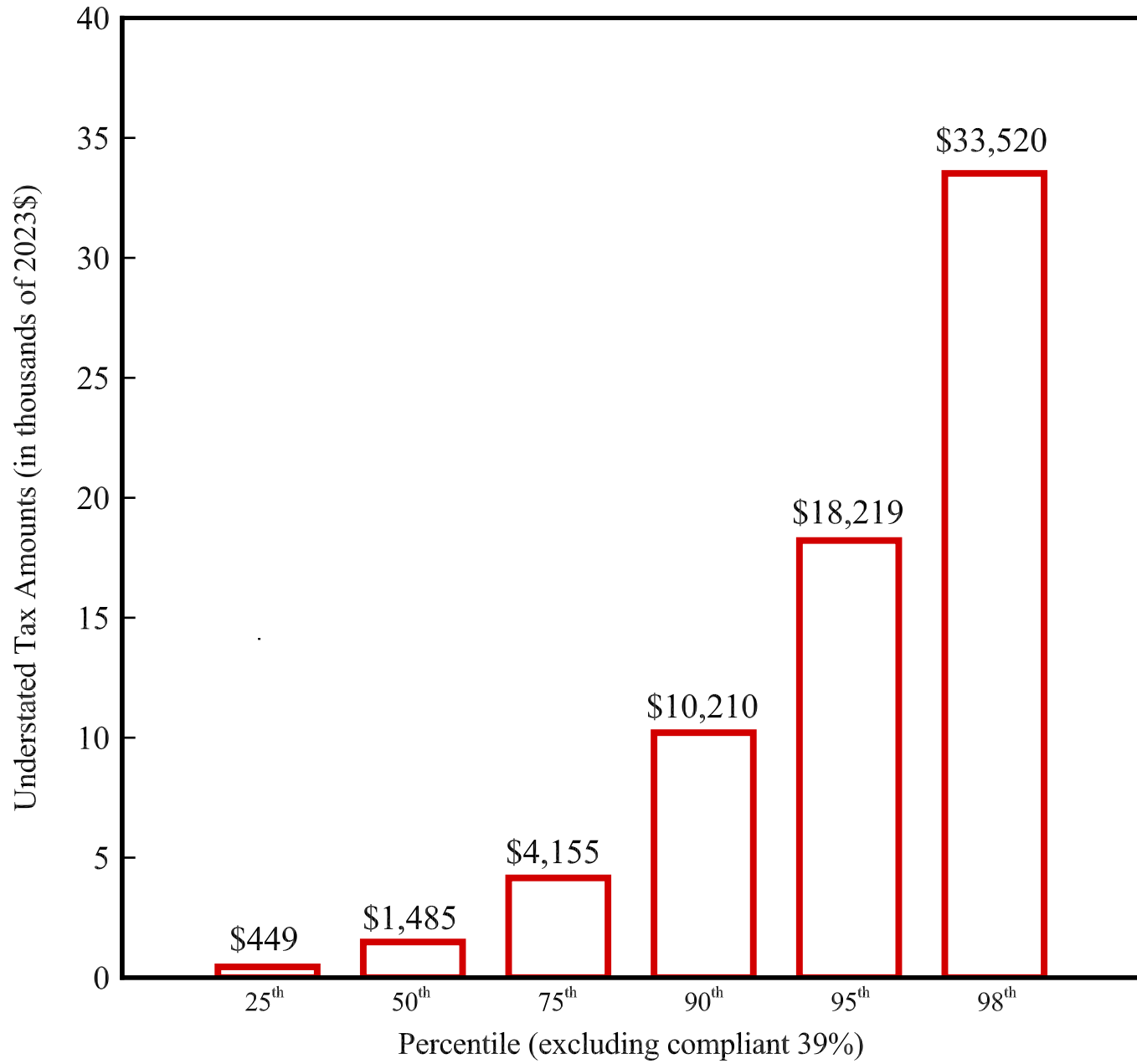


# Proprietors Ranked by Understated Taxes



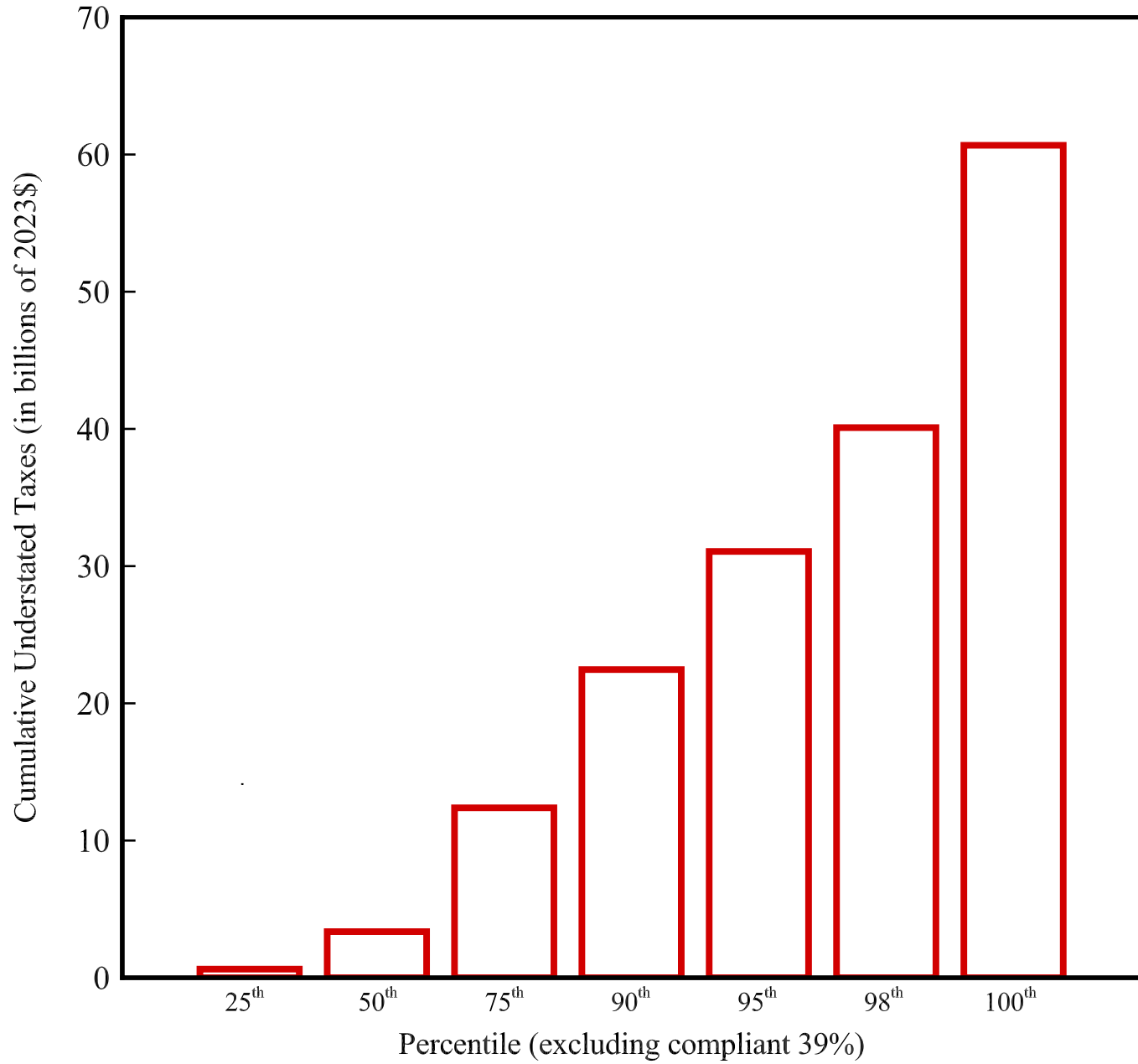


# Proprietors Ranked by Understated Taxes





# Cumulated Understated Taxes





## Nonpecuniary Motives for Compliance

- TAS surveys intended to elicit nonpecuniary motives
- How?
  - Construct samples of sole proprietors
  - Use DIF scores indicating likelihood of audit
  - Group proprietors by DIF score
  - Compare responses of low-DIF and high-DIF groups





## TAS Survey Main Results

- Compare lowest and highest compliance groups
- Where similar:
  - Agree tax rules complicated
  - Know consequences of underreporting
  - Profess moral obligation to pay taxes
- Where different:
  - High-compliance more trusting in IRS/govt
  - High-compliance rely more on preparers

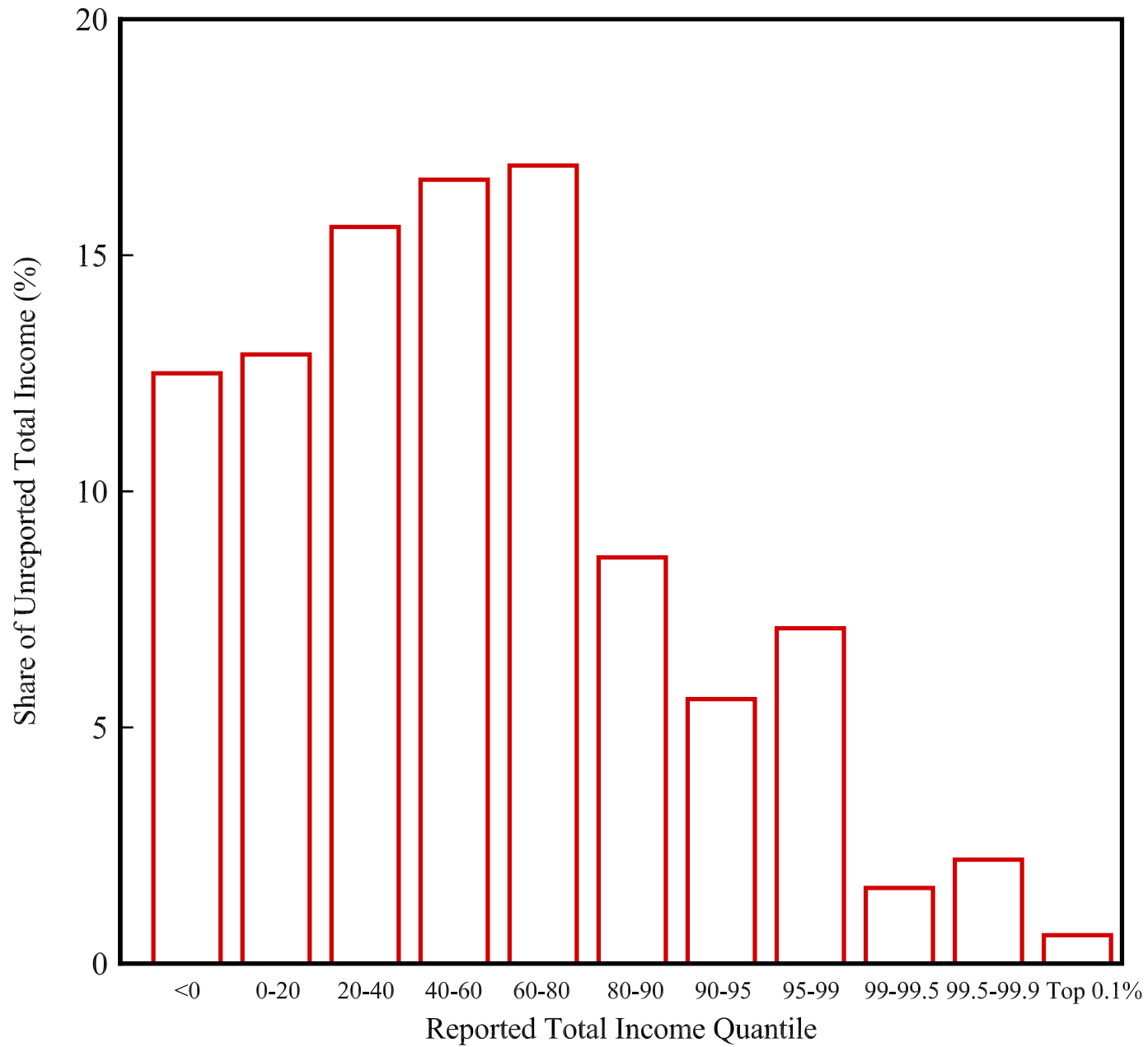


# Does Evasion Occur Across Income Distribution?

- Evidence from NRP random-audit studies (no DCE)
  - Available publicly only for total incomes
  - Shows underreporting across the distribution
- Estimates of very top depend on DCE adjustments



# Shares of Unreported Total Incomes (no DCE)





## Recap: Lessons from IRS Data

- Gross tax gap large and  $\approx 3\%$  of GDP over time
- Underreporting is main source of tax gap
- Underreporting by business owners is most of that
- Underreporting is widespread but concentrated
- Underreporting occurs across the income distribution
- Economic deterrence is only one factor driving compliance



# Theory



## Key Factors

- Occupational choice: paid- or self-employment
- Taxpayer types: always compliant or not
- Noncompliance source: business income underreporting
- Dynamics of tax evasion:
  - Loss of reputation, business brands, customers
  - Recovery of back taxes

⇒ Extends standard model of economic deterrence



# Occupational Choice

- Choose business  $b$  or work  $w$

$$V(s) = \max \{V^b(s), V^w(s)\}$$

$$V^i(s) = \max_x \{U(c, \ell) + \beta \sum_{z', \epsilon'} \pi(z', \epsilon' | z, \epsilon) \mathcal{V}(s')\}$$

where  $s = (a, \kappa, d, z, \epsilon)$  and

- $a$ : financial assets
- $\kappa$ : *sweat capital*, eg, reputation, brands, etc
- $d$ : *back taxes*, eg, accumulated unpaid taxes
- $z$ : productivity in self-employment
- $\epsilon$ : productivity in paid-employment
- $x = [a', \kappa', d', c_p, c_c, \ell, k_p, h_p, h_\kappa, e, c^r, y_b^r]$



# Continuation Value

$$\begin{aligned} \mathcal{V}(a', \kappa', d', z', \epsilon') &= \underbrace{(1 - \Pi(d'))V(a', \kappa', d', z', \epsilon')}_{\text{no audit}} \\ &\quad + \underbrace{\Pi(d')V(a' - f_a(d'), f_r(\kappa'), 0, z', \epsilon')}_{\text{audit}} \end{aligned}$$





# Continuation Value

$$\mathcal{V}(a', \kappa', d', z', \epsilon')$$

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↑  
Probability of audit



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↑                      ↗

Probability of audit and fines depend on  $d'$



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$$+ \underbrace{\Pi(d')V(a' - f_a(d'), f_r(\kappa'), 0, z', \epsilon')}_{\text{audit}} \uparrow$$

Audit results in reputational losses



# Business Owner's Technologies

- Goods and services:  $y_p = z f_p(\kappa, k_p, h_p)$ 
  - $z$  = productivity in self-employment
  - $\kappa$  = sweat capital
  - $k_p$  = rented physical capital
  - $h_p$  = owner time in production
- Sweat investment:  $x_\kappa = f_\kappa(h_\kappa, e)$ 
  - $h_\kappa$  = owner time in brand building
  - $e$  = owner expenses



# Business Owner's Constraints

- Budget

$$a' = [(1+r)a + y_b - T^b(y_b^r) - (1+\tau_c)(c_c + pc_p) + \chi] / (1+\gamma)$$

- Sweat capital

$$\kappa' = [(1 - \delta_\kappa)\kappa + f_\kappa(h_\kappa, e)] / (1 + \gamma)$$

- Back taxes

$$d' = [(1 - \delta_d)d + f_d(c^r)] / (1 + \gamma)$$

- Borrowing

$$a' \geq f_a(d')$$



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↑

↗

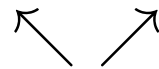
next period and current assets



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true and reported income

$$y_b = py_p - (r + \delta)k_p - e, \quad y_b^r = y_b - (1 + \tau_c)c^r$$





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↑ ↗

taxes on business and consumption



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goods produced by C-corps  
and pass-thrus,  $c = \text{ces}(c_c, c_p)$



# Business Owner's Constraints

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↑

transfers



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↑

sweat investment (shown earlier)



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↑

current misreporting:  $y_b - y_b^r = (1 + \tau_c)c^r$



## Business Owner's Constraints

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## Close the Model

- Standard dynamic program for workers, except
  - Sweat capital decays without use
  - Back taxes not forgiven
- Standard dynamic program for C corporations
- Public financing (G&S plus transfers) with
  - Taxes on consumption and all forms of income
  - Fines if caught evading taxes

(Details in slide deck appendix)



# Qualitative Predictions



# Predictions of Increased Enforcement

- Lower precautionary motives
  - Financial assets used to pay future fines
  - Borrowing constraints less binding
- Lower sweat capital stocks
  - Brand assets lost with exposed tax evasion
  - Business ages lower with more exit/entry
  - Business productivity higher due to selection



# Quantitative Results



## Key Compliance Parameters

- Audit probability,  $\Pi(d') = \pi$ ,  $\pi$  varied
- Fines,  $f_a(d) = \bar{p}d$ ,  $\bar{p} = 4$
- Reputational cost,  $f_r(\kappa) = 0$  if non-compliant
- Underreporting,  $f_d(c^r) = \tau_b(1 + \tau_c)c^r$ ,  $\tau_c = .065$ ,  $\tau_b = .4$
- Back taxes depreciation,  $\delta_d = 20\%$

*Note:* See paper for full calibration



## Comparative Statics

- Vary audit probability  $\pi$
- Record impacts for owners by type



## Fraction of Population

Owner type:	% Change from $\pi = 1\%$ to			
	2%	3%	5%	7%
Non-compliant	-21	-35	-60	-70
Compliant	11	23	43	45
All owners	-6	-9	-12	-17

⇒ Large compositional shift





## Financial Assets (a)

Owner type:	% Change from $\pi = 1\%$ to			
	2%	3%	5%	7%
Non-compliant	-4	-9	-29	-57
Compliant	5	12	28	39
All owners	-10	-18	-30	-36

⇒ Large drop in precautionary saving



# Productivity ( $z$ )

Owner type:	% Change from $\pi = 1\%$ to			
	2%	3%	5%	7%
Non-compliant	9	16	25	27
Compliant	0	0	-1	-2
All owners	6	9	10	11

$\Rightarrow$  Large increase in productivity due to selection



## Sweat Capital ( $\kappa$ )

Owner type:	% Change from $\pi = 1\%$ to			
	2%	3%	5%	7%
Non-compliant	-9	-14	-37	-31
Compliant	12	13	21	21
All owners	-4	-9	-15	-12

⇒ Large drop in business assets with more audits



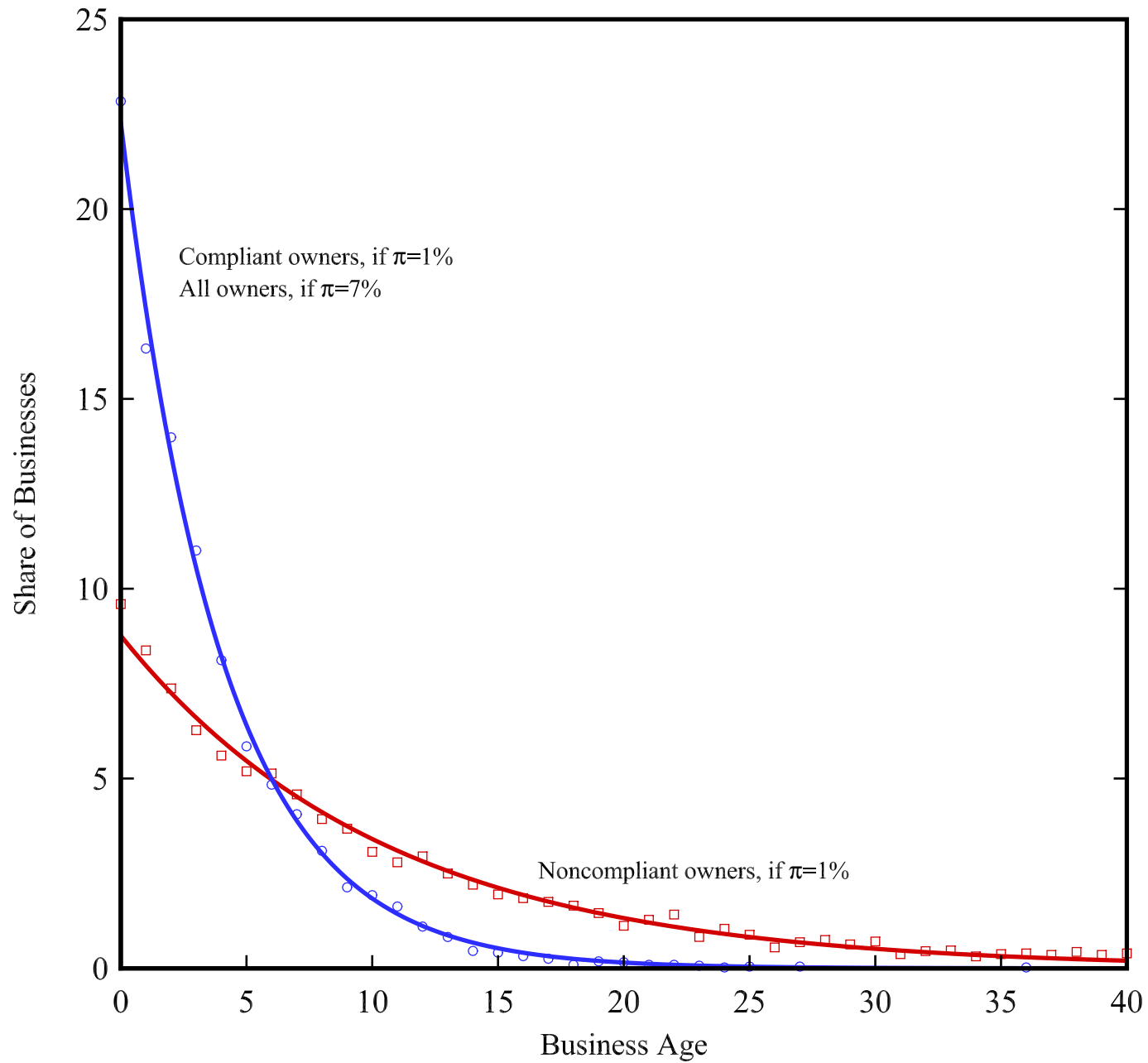
## Business Age

Owner type:	% Change from $\pi = 1\%$ to			
	2%	3%	5%	7%
Non-compliant	-33	-50	-64	-68
Compliant	5	8	15	18
All owners	-30	-42	-49	-49

⇒ Large drop in age with more audits, less capital



# Business Age Distributions ( $\pi=1\%$ and $7\%$ )





# Distributional Impacts

- Two rankings of interest:
  - By misreporting rates:  $100(y_b - y_b^r)/y_b$
  - By business receipts:  $py_p$
- Looking for patterns of underreporting
  - Few owners account for most cheating
  - Cheating occurs across the income distribution



## Rank Owners by Underreporting ( $\pi = 2\%$ )

% Deviations	% of Income Underreported				
	None	<80	80-90	90-99	>99
Business age	-37	-18	19	4	67
Financial assets	-40	-63	-30	-4	79
Sweat capital	-21	63	59	51	23
Productivity	7	11	14	13	-16
True income	-10	111	107	93	-7
% Owners	59	2	2	4	33

⇒ Concentrated, but too many able to get income to 0



## Rank Owners by Receipts ( $\pi = 2\%$ )

% Deviations	Quintiles of Receipts				
	(1)	(2)	(3)	(4)	(5)
Business age	-21	6	-21	14	21
Financial assets	19	12	-1	-6	-23
Sweat capital	-57	-13	-15	36	49
Productivity	-21	-17	10	14	14
True income	-113	-68	5	72	104
% Underreporting	32	47	26	36	57

⇒ Cheating occurs throughout the size distribution





# Policy Counterfactuals

- Two ways to raise same revenues
  - Higher enforcement:  $\pi = 2\% \rightarrow \pi = 5\%$
  - Higher tax rate on business:  $\tau_b = 40\% \rightarrow \tau_b = 47\%$
- Raise revenues by 3% relative to  $\pi = 2, \tau_b = 40$  baseline



# Enforcement vs Taxation

% Change in:	More Audits $\pi=5$ vs 2%	Higher Tax $\tau_b=47$ vs 40%
# of Owners	-7	-4
Non-compliant	-50	12
Compliant	29	-18
Business age	-28	16
Financial assets, $a$	-22	14
Sweat capital, $\kappa$	-11	6
Back taxes, $d$	-66	44
Productivity, $z$	6	-3
Business income, $y_b$	4	4



## Bottom Line

- Higher enforcement vs taxation
  - Most evident in composition of businesses/owners
  - Not evident in aggregate business income
- Need transitional dynamics to do proper welfare analysis



## Next Steps

- Data: gather relevant IRS micro data
  - Current NRP studies only work with 1040
  - Want to expand analysis to business filings
- Theory: add transitional dynamics
  - Current analysis is steady state
  - Want to analyze Inflation Reduction provisions
  - Want to do full welfare analysis with transition



# Appendix



## Dynamic Program for Workers

- Workers choose  $x = [a', c_p, c_c, \ell]$  to solve

$$V^w(s) = \max_x \{U(c, \ell) + \beta \sum_{z', \epsilon'} \pi(z', \epsilon' | z, \epsilon) \mathcal{V}(s')\}$$

subject to

$$a' = [(1 + r)a + w\epsilon h_w - T^w(w\epsilon h_w) - (1 + \tau_c)(c_c + pc_p) + \chi]/(1 + \gamma)$$

$$\kappa' = (1 - \lambda_\kappa)\kappa/(1 + \gamma)$$

$$d' = (1 - \lambda_d)d/(1 + \gamma)$$

$$1 = \ell + h_w$$



# Dynamic Program for Corporations

- Corporations choose  $x_c, n_c$  to solve

$$V^c(k_c) = \max \left\{ (1 - \tau_d)d_c + \frac{1 + \gamma}{1 + r} V^c(k'_c) \right\}$$

subject to

$$d_c = AF(k_c, n_c) - wn_c - x_c - \tau_p(y_c - wn_c - \delta_k k_c)$$

$$x_c = (1 + \gamma)k'_c - (1 - \delta_k)k_c$$



# Government Budget Constraint

$$\begin{aligned} g + \chi + (r - \gamma)b &= \tau_c \int (c_{ci} + pc_{pi}) di + \\ &+ \tau_d(y_c - wn_c - (\gamma + \delta_k)k_c - \tau_p(y_c - wn_c - \delta_k k_c)) \\ &+ \tau_p(y_c - wn_c - \delta_k k_c) + \int T^n(w\epsilon_i n_i) di \\ &+ \int T^b(y_{ri}^b) di + \int \mathbf{1}_i f_a(d_i) di \end{aligned}$$