

The Aggregate Implications of Innovative Investment

BY A. ATKESON AND A. BURSTEIN

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- If policy changed to induce more innovation,
- What happens to
 - Output
 - Productivity
 - \circ Welfare?



- Develop model nesting many others
- Use discipline of national accounts



- Welfare gains are potentially huge
- But, results very sensitive to
 - Model choice
 - Parameter estimates



- AB's main result doesn't rely on cross-section data
- Aggregate implications of innovative investment:
 - Can estimate medium-run growth
 - Can't yet estimate long-run growth or welfare



• Firm output:

$$y_t = K_{It}^{\rho} (k_{Tt}^{\alpha} k_{It}^{\gamma} l_t^{1-\alpha-\gamma})$$

• Capital accumulation

$$k_{Tt+1} = (1 - \delta_T)k_{Tt} + x_{Tt}$$
$$k_{It+1} = (1 - \delta_I)k_{It} + \underbrace{A_{rt}K_{It}^{\phi - 1}x_{It}}_{y_{rt}}$$



• Given α, γ , define:

 $\log Z_t = \log Y_t - \alpha \log K_{Tt} - (1 - \alpha - \gamma) \log L_t$

• Then growth rates are:

 $g_{Zt} = (\rho + \gamma)g_{K_{It}}$ $g_{K_{It}} = \log(1 - \delta_I + Y_{rt}/K_{It})$

• And AB's elasticity is:

$$\epsilon_{zr} = \frac{g_{Zt} - \bar{g}_Z}{\log Y_{rt} - \log \bar{Y}_r} \approx (\rho + \gamma) \left(\frac{\exp \,\bar{g}_{K_I} - 1 + \delta_I}{\exp \,\bar{g}_{K_I}}\right)$$



$$\epsilon_{zr} \approx (\rho + \gamma) \left(\frac{\exp \,\bar{g}_{K_I} - 1 + \delta_I}{\exp \,\bar{g}_{K_I}} \right)$$

- $ho + \gamma = 1/3$ (based on variety models) $\bar{g}_Z = .0123$ (based on BEA/BLS data) $\bar{g}_{K_I} = .0369$ (from definition) δ_I ?
 - 0.0, $\epsilon_{zr} = .012$.15, $\epsilon_{zr} = .06$ 1.0, $\epsilon_{zr} = 1/3$



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 \Rightarrow use investment/value ratio (X_I/V_I) instead



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 - $\Rightarrow \text{ use investment/value ratio } (X_I/V_I = .08)$ $X_I: \text{ NIPA+imputation for entrants}$ $V_I: \text{ dividends/(interest rate growth rate)}$



$$\epsilon_{zr} \approx (\rho + \gamma) \left(\frac{\exp \bar{g}_{K_I} - 1 + \delta_I}{\exp \bar{g}_{K_I}} \right) \approx (\rho + \gamma) \frac{X_I}{V_I}$$

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- $\epsilon_{zr} = 2.7\%$
 - $\circ~$ Used no information from LBD or GHK
 - Relied on only one dubious parameter (ρ)



- $\epsilon_{zr} = 2.7\%$
 - $\circ~$ Used no information from LBD or GHK
 - Relied on only one dubious parameter (ρ)
- What does this imply for future growth and welfare?





10% Increase in Innovation Investment





10% Increase in Innovation Investment





10% Increase in Innovation Investment



- To rationalize both
 - \circ Observed growth in Y, L and
 - $\circ~$ Large negative spillovers
- Requires high growth in A_r



• Recall

$$y_t = K_{It}^{\rho} (k_{Tt}^{\alpha} k_{It}^{\gamma} l_t^{1-\alpha-\gamma})$$
$$y_{rt} = A_{rt} K_{It}^{\phi-1} x_{It}$$

• Growth in output (with $\phi = 1$):

$$\underbrace{\overline{g}_{Y}}_{.025} = \underbrace{\underbrace{(1-\alpha)(2-\phi) - (\rho+\gamma)}_{.762}}_{.762} \underbrace{\underbrace{g_{A_{r}}}_{.033}}_{.033} + \underbrace{\frac{(1-\phi)(1-\alpha-\gamma)}{(1-\alpha)(2-\phi) - (\rho+\gamma)}}_{0} \underbrace{\underbrace{g_{L}}_{.008}}_{0}$$



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• Growth in output (with $\phi = -1.6$):

$$\underbrace{\overline{g}_{Y}}_{.025} = \underbrace{\underbrace{(1-\alpha)(2-\phi) - (\rho+\gamma)}_{.137}}_{.137} \underbrace{\underbrace{g_{A_{r}}}_{.144}}_{.144} + \underbrace{\frac{(1-\phi)(1-\alpha-\gamma)}{(1-\alpha)(2-\phi) - (\rho+\gamma)}}_{.672} \underbrace{g_{L}}_{.008}$$



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Choice of ϕ also matters for welfare...



- Depend importantly on
 - \circ Spillovers
 - \circ Appropriation
 - ... which are both hard to estimate



• Proportion κ stolen

$$k_{It+1} = (1 - \delta_I)k_{It} + (1 + \kappa)q_{rt}x_{It} - \kappa q_{rt}k_{It}\frac{X_{It}}{K_{It}}$$

- -

- New impact elasticity: $\epsilon_{zr}^* = \epsilon_{zr}/(1+\kappa)$
- How to interpret κ ?
 - Weak IP protection?
 - Quid pro quo policy?
- How to measure κ ?



• No appropriation:

1% rise in X_I/Y

 $\Rightarrow~2.3$ to 15% rise in welfare depending on ϕ

• With appropriation:

1% rise in X_I/Y

 \Rightarrow possibly negative welfare!

• Optimal policy may involve barriers to new firms, products



- Need estimates for some key parameters
- AB on right track
 - $\circ~$ Match theory to NIPA
 - Should look at cross-country evidence
- Don't see that they need LBD or GHK