



# QUANTIFYING EFFICIENT TAX REFORM

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## Question

- How large are welfare gains from efficient tax reform?
  - Baseline:
    - Positive economy matched to administrative data
  - Reform:
    - Pareto improvements on efficient frontier (full)
    - Optima given set of policy tools (partial)



Idea in a Picture



## Idea in a Picture

- Start with baseline OLG economy:
  - Incomplete markets
  - Heterogeneous households
  - Consumption, labor, saving decisions
  - Parameters/policies for actual economy
- Compute remaining lifetime utilities ( $v_j$ )

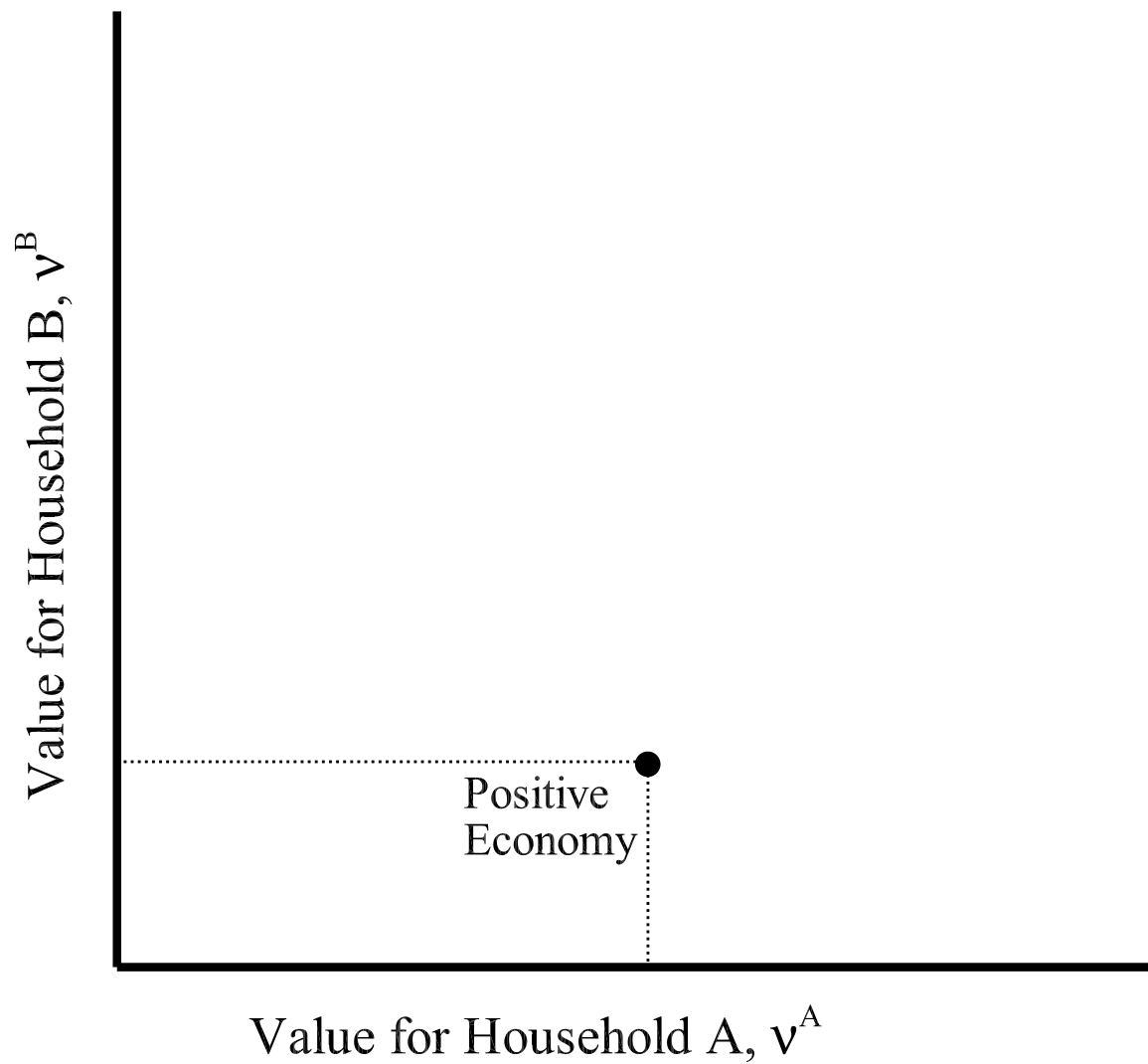


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- Compute remaining lifetime utilities ( $v_j$ )
- Let's draw this for 2 households...



# Idea in a Picture



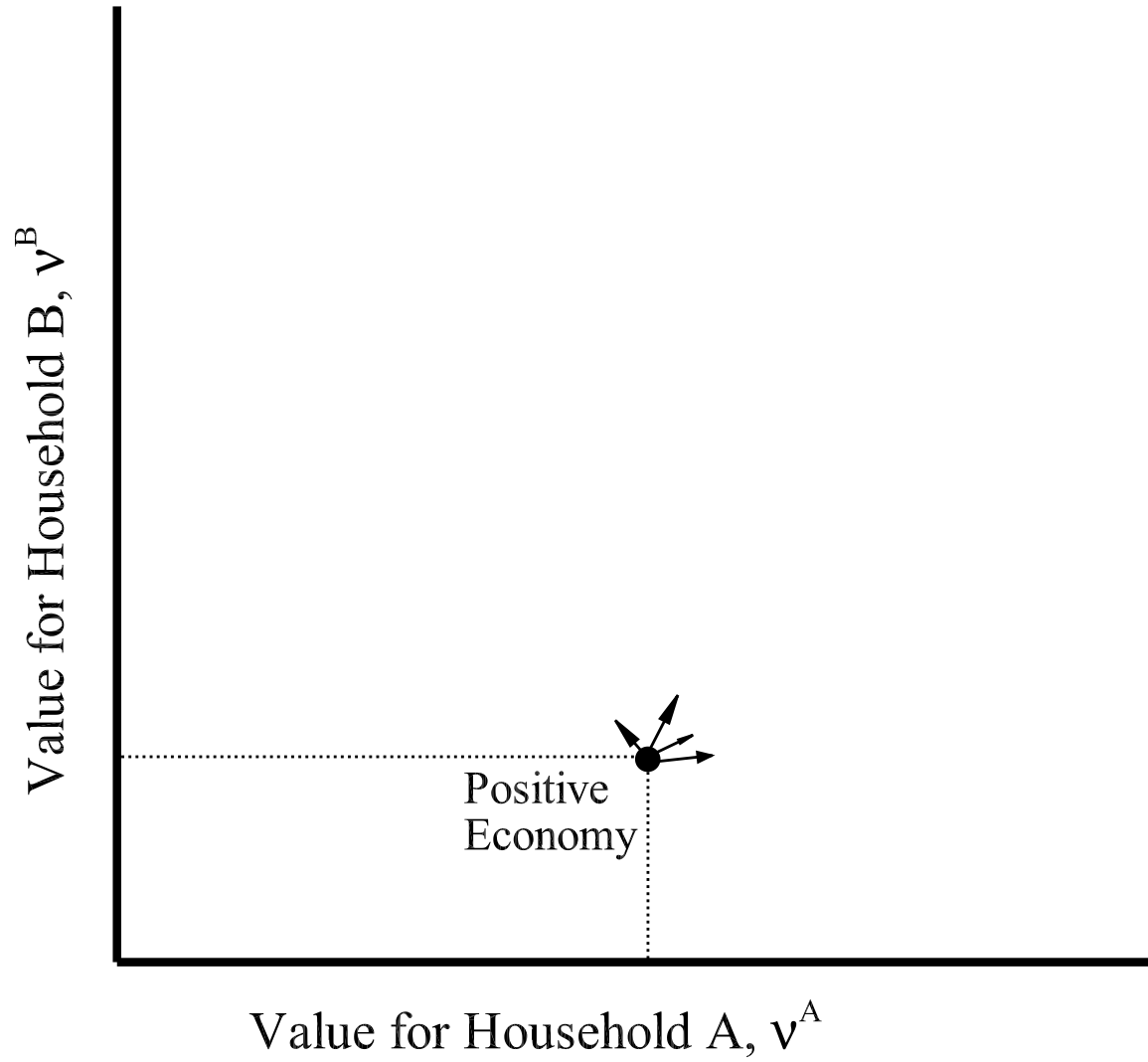


## Idea in a Picture

- Typical starting point for most analyses
  - With constraints on policy instruments
  - Do counterfactuals or restricted optimal (“Ramsey”)
  
- Let’s draw this in the picture



# Idea in a Picture





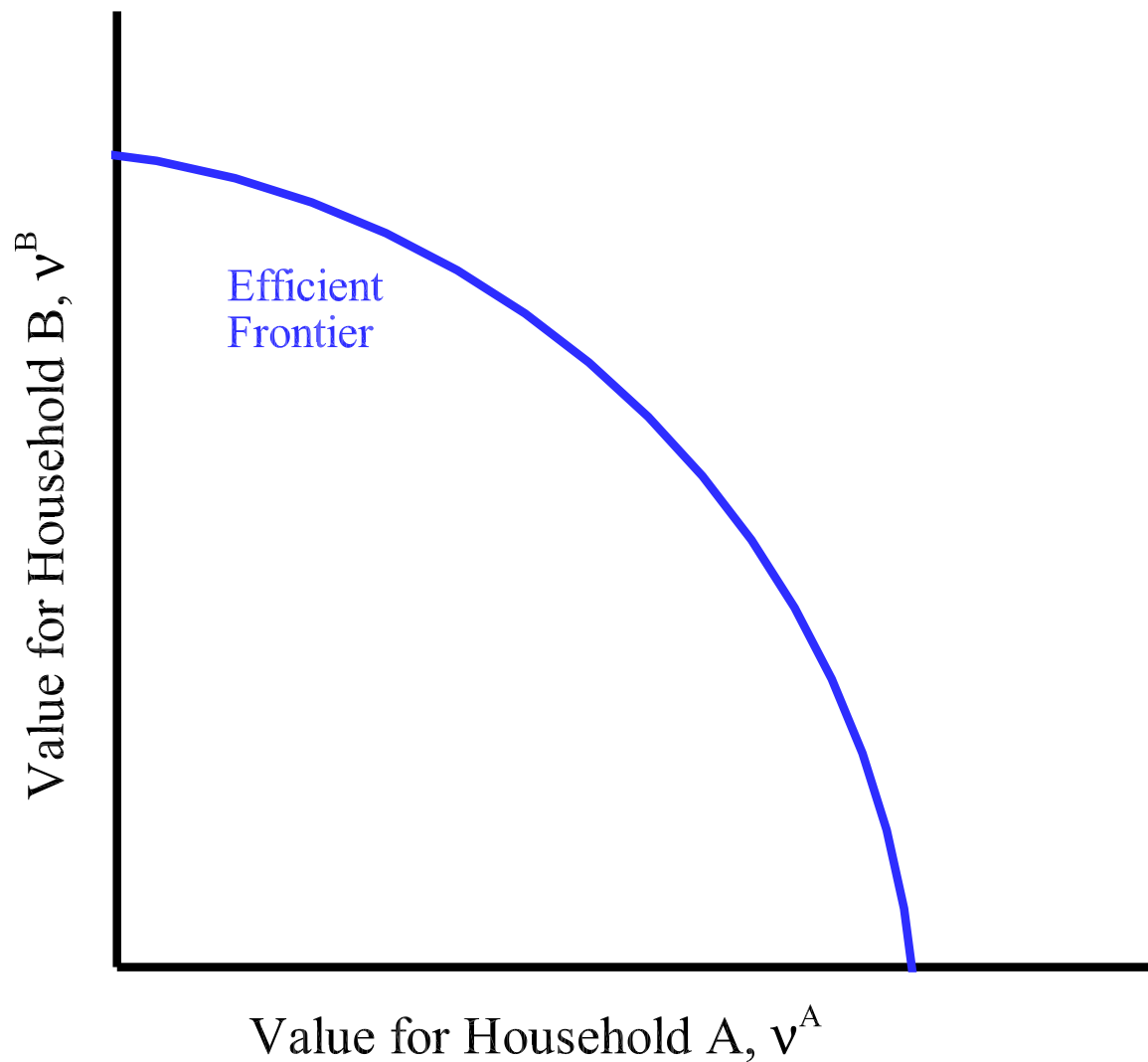


## Idea in a Picture

- Not typical starting point for studies in Mirrlees tradition
  - With constraints on information sets
  - Characterize efficient allocations and policy “wedges”
  
- Let’s draw this in the picture



# Idea in a Picture



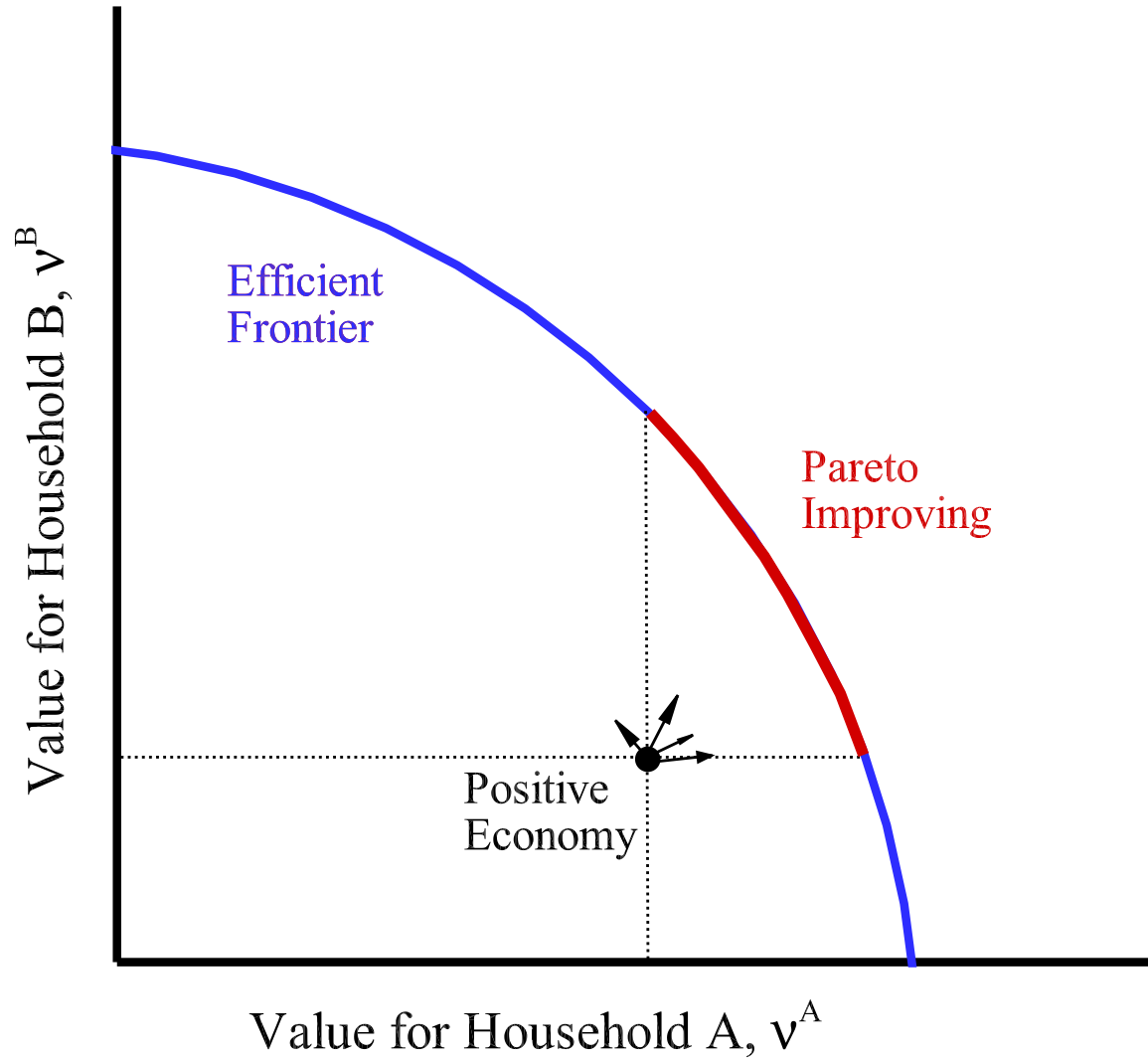


## Idea in a Picture

- This paper quantifies gains from:
  - Full Pareto-improving reform a la Mirrlees
  - Partial Pareto-improving reform a la Ramsey
  - Adding early-life transfer informed by Mirrlees
- Let's draw this in the picture

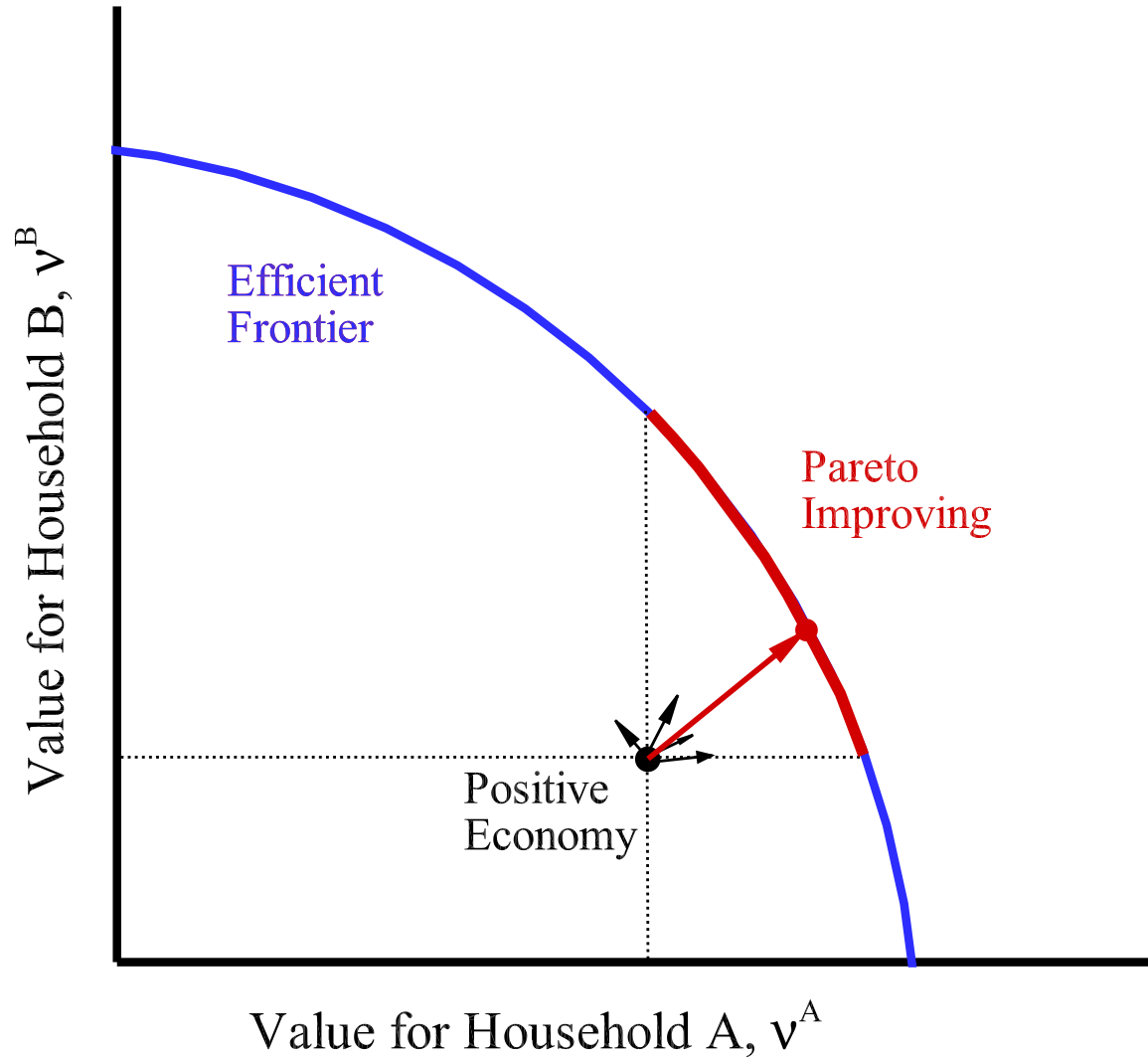


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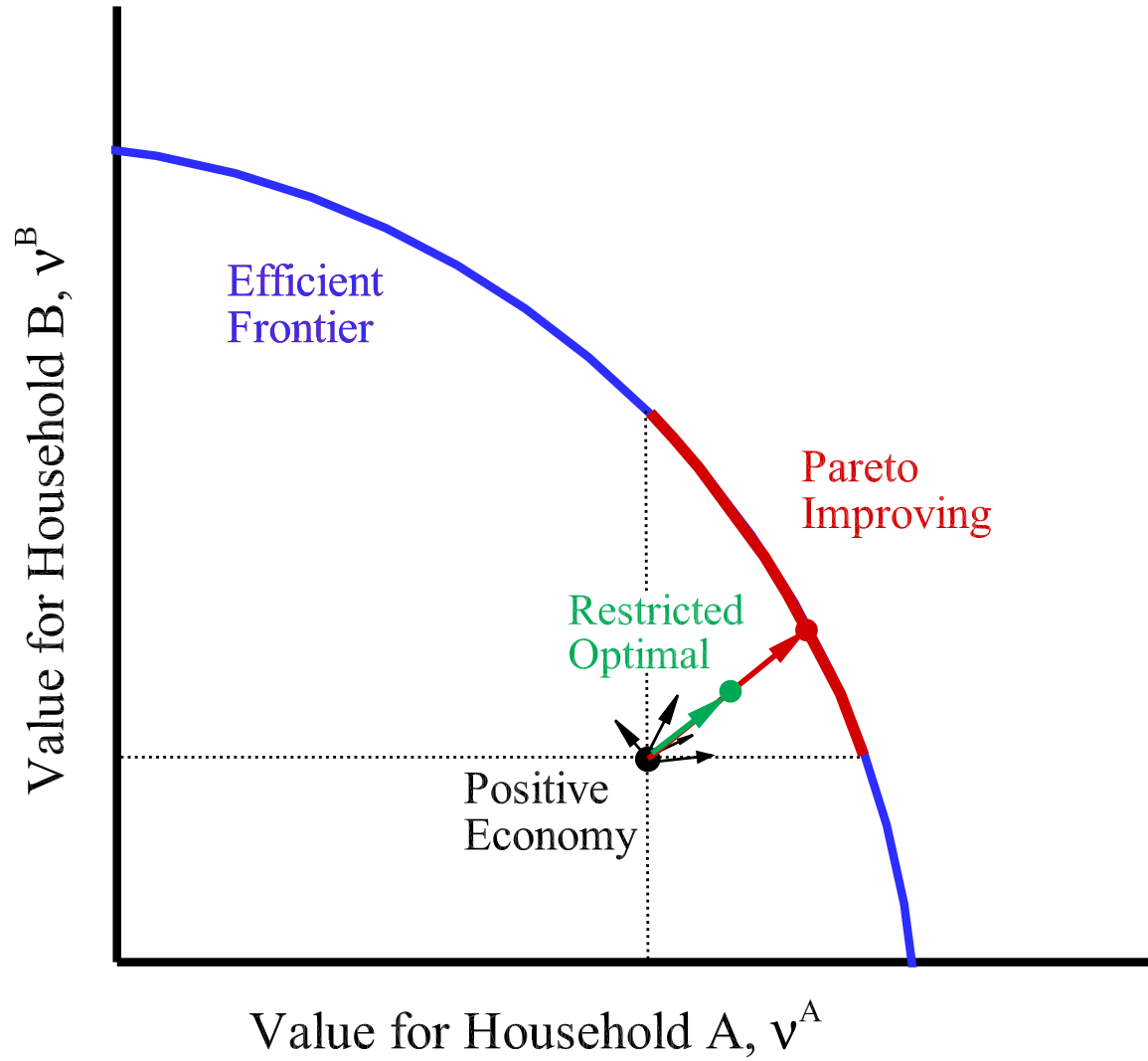


# Idea in a Picture





# Idea in a Picture





## Our Approach

- Solve equilibria for positive economy (●)
  - Inputs: fiscal policy and wage processes
  - Outputs: values under current policy
- Solve planner problem next (●)
  - Inputs: values under current policy
  - Outputs: labor and savings wedges and welfare gains
- Use results to inform current policy and reforms (●)



## Main Findings

- Maximum consumption equivalent gains (future cohorts):
  - 21% for baseline parameterization (●)
  - 5% attained with current policies (●→)
  - 7% attained with early-life transfer (●)
- Decompose by comparing allocations:
  - Consumption: level  $\uparrow$  and variance  $\downarrow$  for all groups
  - Leisure: level  $\downarrow$  and variance  $\uparrow$  for all groups

*Note:* Working on computing gains for *all* cohorts





## Main Findings

- Maximum consumption equivalent gains (future cohorts):
  - 21% for baseline parameterization (●)
  - 5% attained with current policies (still hillclimbing)
  - 7% attained with early-life transfer (still hillclimbing)
- Decompose by comparing allocations:
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*Note:* Working on computing gains for *all* cohorts



## Contributions to Literature

- Theory and application of income tax design (●→)
  - ⇒ Using administrative data from NL, go to (●)
- Pareto-improving reforms with fixed types  
Hosseini-Shourideh (2019)
  - ⇒ Extend analysis to add dynamic risks
- Theory behind dynamic taxation and redistribution (●)  
Kapicka (2013), Farhi-Werning (2013), Golosov et al. (2016)
  - ⇒ Link OLG (●) to planner (●) in full GE



## Positive Economy (●)

- Open OLG economy a la Bewley
- Household heterogeneity in:
  - Age
  - Education (observed, permanent)
  - Productivity (private, stochastic)
  - Unemployment risk (in progress)
  - Marriage and divorce risk (in progress)
- Transfers and taxes on consumption, labor income, assets



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  - Transfers and taxes on consumption, labor income, assets
- ⇒ Estimated with administrative data for the Netherlands



## Reform Problem (•)

- Take inputs from positive economy:
  - Parameters of preferences and technologies
  - Wage profiles and shock processes
  - Values under current policy ( $v_A, v_B, \dots$ )
- Compute maximum consumption equivalent gain

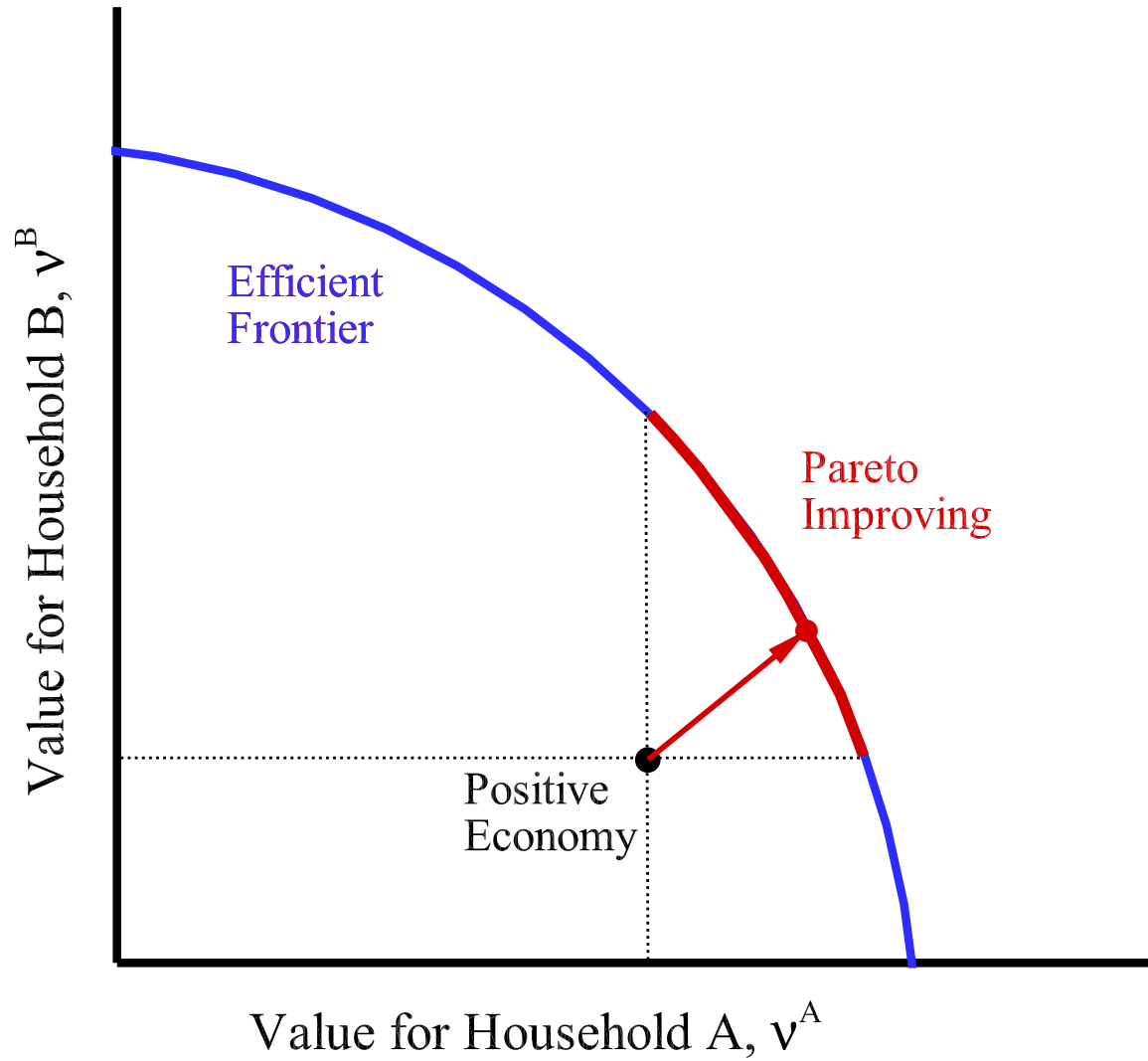


## Notion of Efficiency

- Our focus is Pareto-improving reforms:
  - There is no alternative allocation that is
    - Resource feasible (only so much to go around)
    - Incentive feasible (induces truthful reports)
  - Making all better off and some strictly better off
- Will report gain assuming same percentage for all

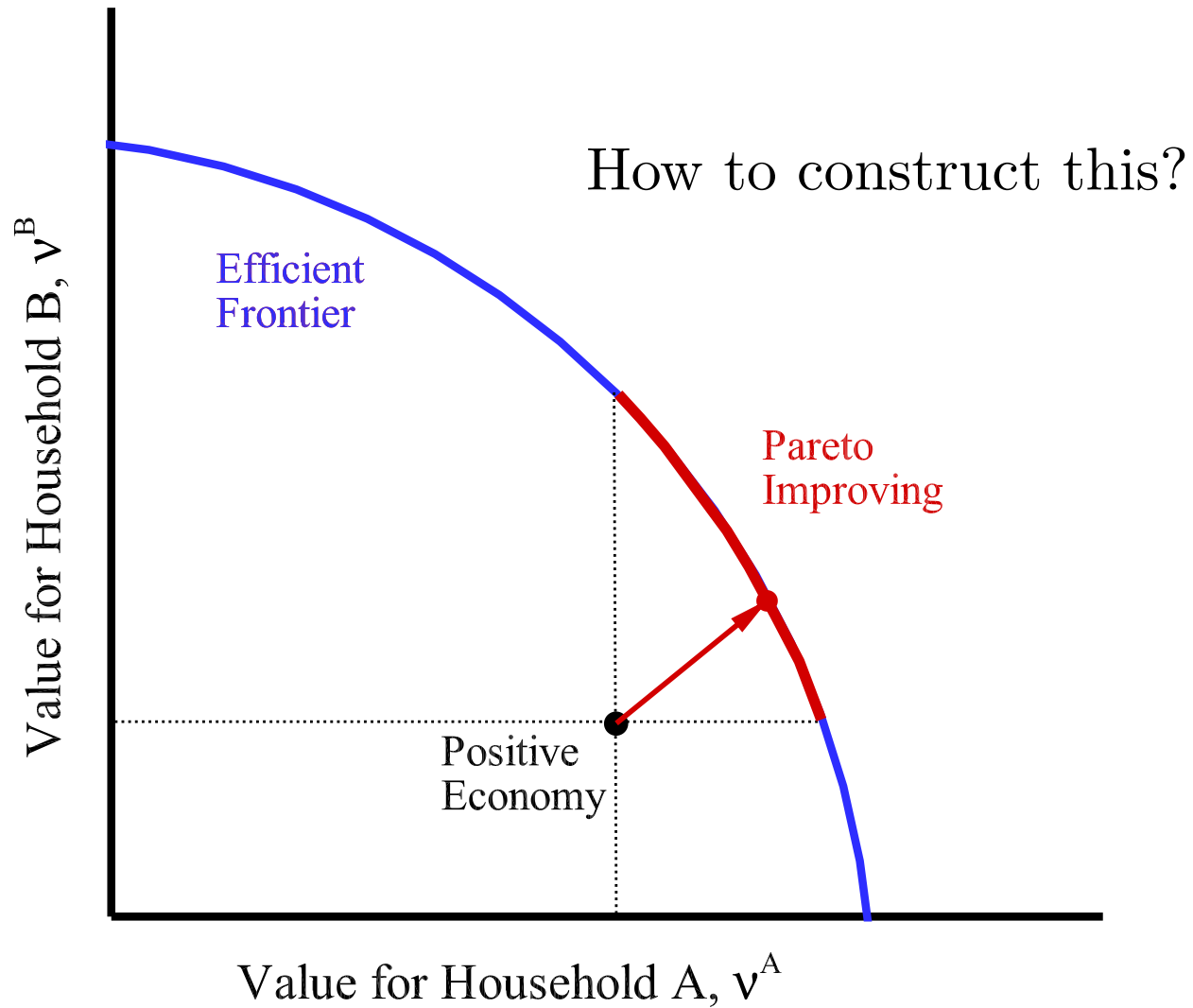


# Pareto-improving Reforms





# Pareto-improving Reforms







## Planner Problem in Words

- Maximize present value of aggregate resources
- subject to
  - Incentive constraints for every household and history
  - Values delivered exceed that of positive economy
- GE: total resources  $\leq$  to that in positive economy



## Planner Problem in Practice

- Exploit separability to solve household by household
- Include only local downward incentive constraints
- Verify numerically that all ICs satisfied
- Solve recursively by introducing additional states:
  - Promised value for truth telling
  - Threat value for local lie



# Planner Problem Deliverables

- Welfare gains
  - Total consumption equivalent
  - Decomposition
- Wedges

*Note:* Working on sensitivity of planner results



# Netherlands

- Merged administrative data, 2006-2014
  - Earnings from tax authority
  - Hours from employer provided data
  - Education from population survey
- National accounts
- Tax schedules

*Note:* Big advantage is data for computing shocks

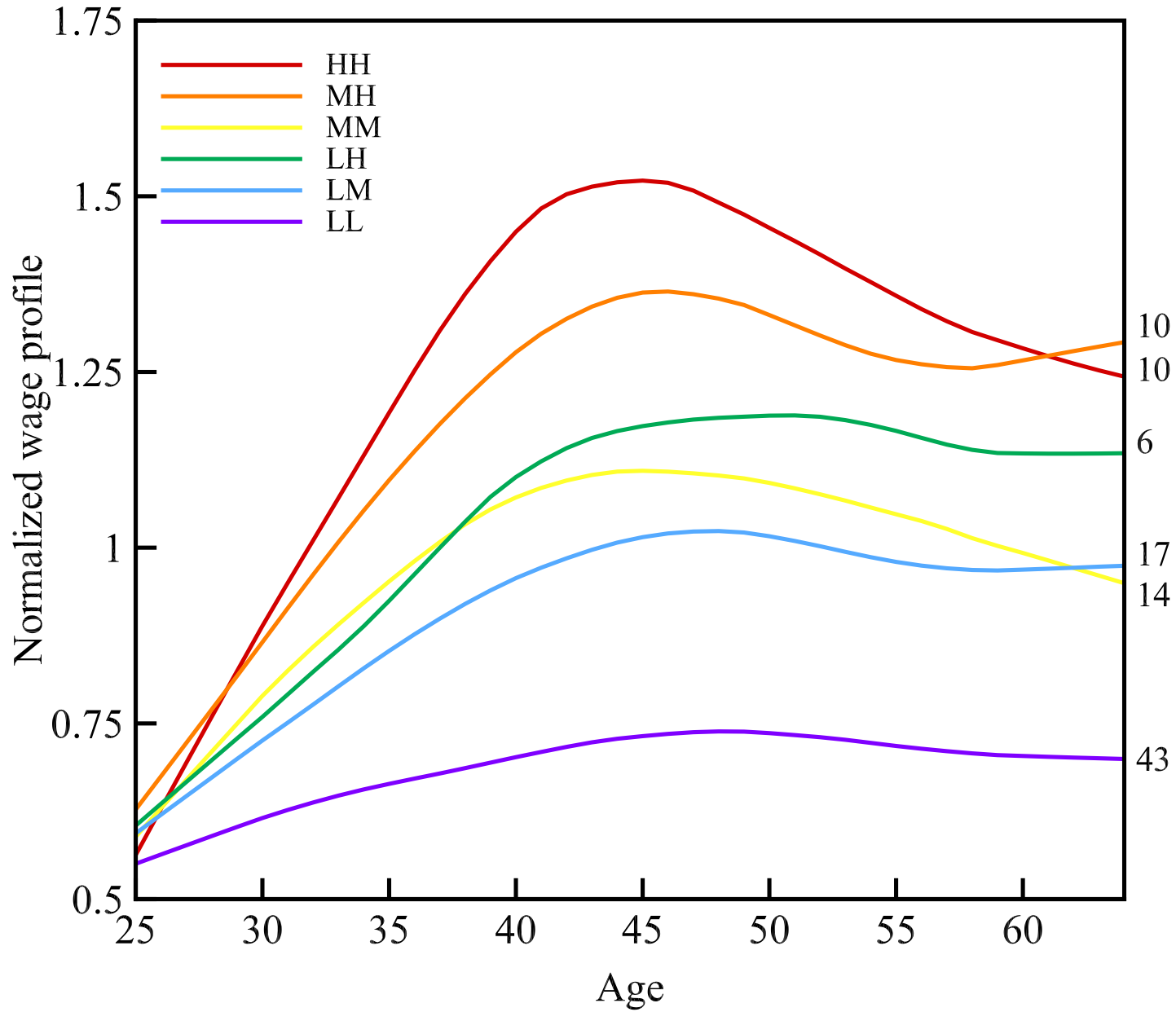


# Estimation of Wage Processes

- Construct hourly wages  $W_{ijt}$  ( $j$ =age,  $t$ =time)
- Classify degrees:
  - High school or practical (Low)
  - University of applied sciences (Medium)
  - University (High)
- Bin households into 6 groups (HH, HM, ...)
- Construct residual wages  $\omega_{ijt}$ :
  - $\log W_{ijt} = A_t + X_{ijt} + \omega_{ijt}$
  - Estimate AR(1) process for idiosyncratic risk



# Wage Profiles



(See paper for estimated wage processes)



## An Aside

- Government:
  - Can *ex-post* infer type from choices
  - Can't *ex-ante* observe type
- But, can design policy to *induce* truthful reporting of type



## Other Key Parameters

- Number of productivity types
- Preferences
- Status quo policy

Baseline: 20 types, log preferences, NL wages & policy

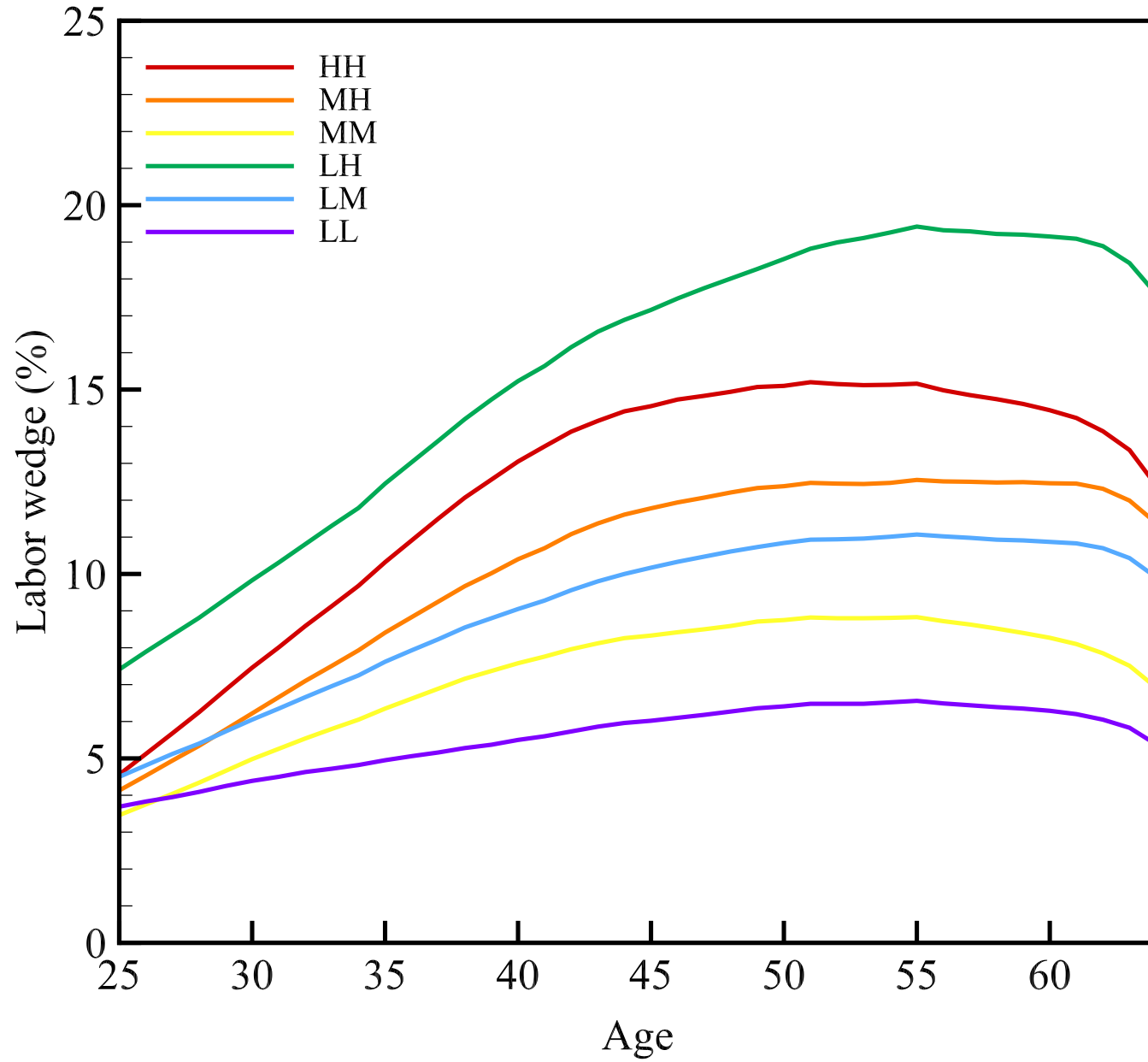




# Results

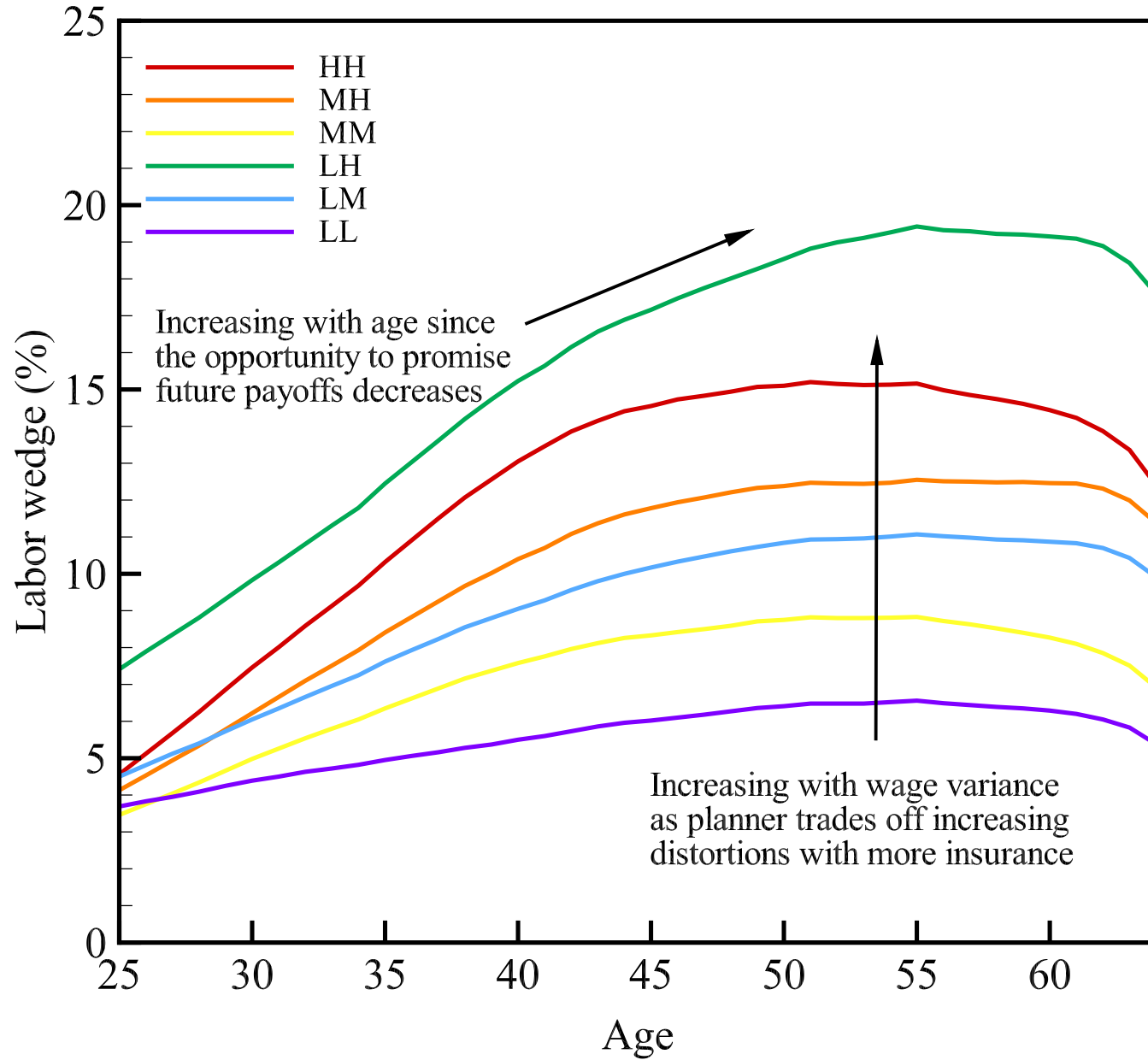


# Labor Wedges





# Labor Wedges





## Welfare, (●) vs (●)

- Consumption equivalent gain of 21% for future cohorts
- Large but maybe not surprising given:
  - Tax rates in NL over 40%
  - Tax wedges of planner in 4% to 20% range

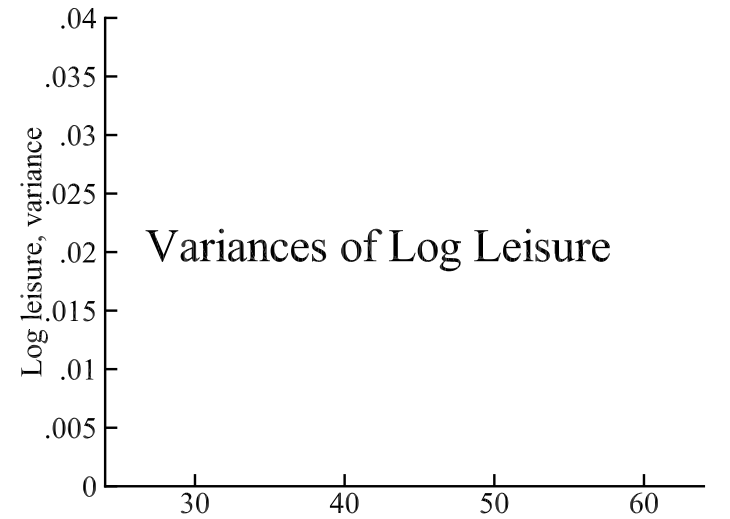
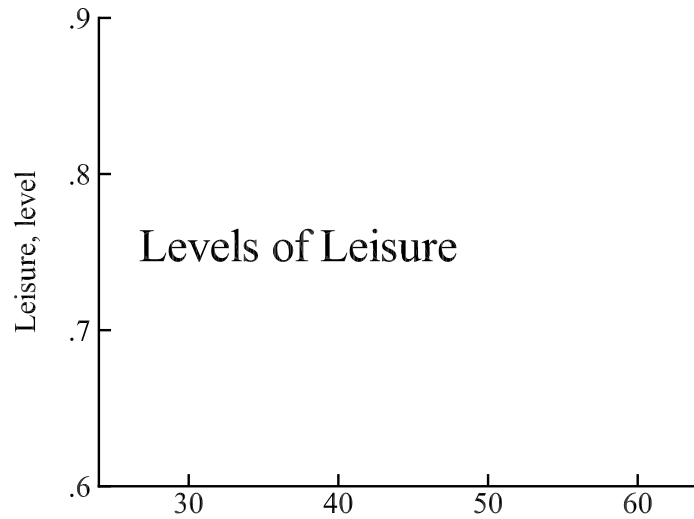
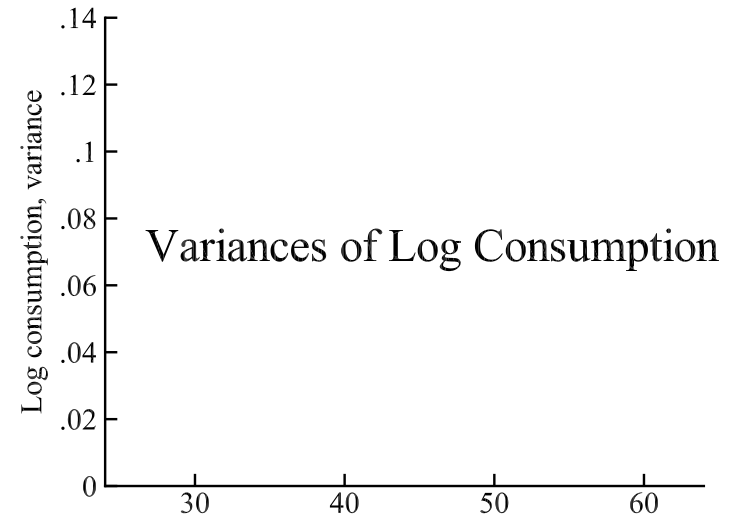
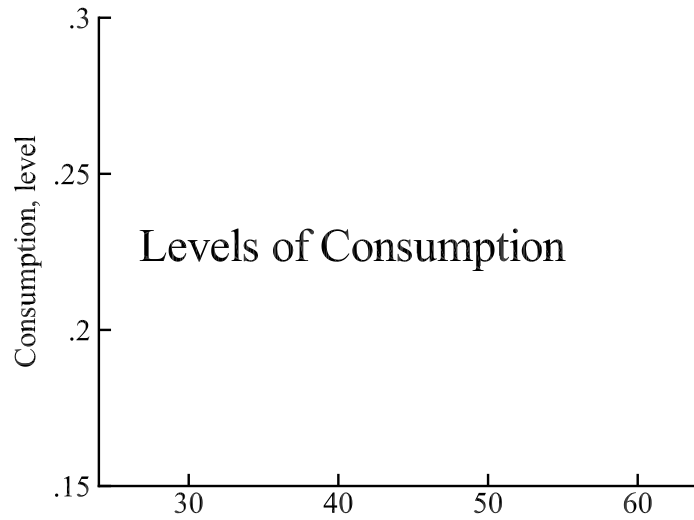


## Comparing Allocations, ( $\bullet$ ) vs ( $\bullet$ )

- Consumption: level  $\uparrow$  and variance  $\downarrow$  for all groups
- Leisure: level  $\downarrow$  and variance  $\uparrow$  for all groups
- Intuition from simple static model:
  - With no insurance:  $c$  varies,  $\ell$  constant
  - With full insurance:  $c$  constant,  $\ell$  varies
- What about magnitudes?

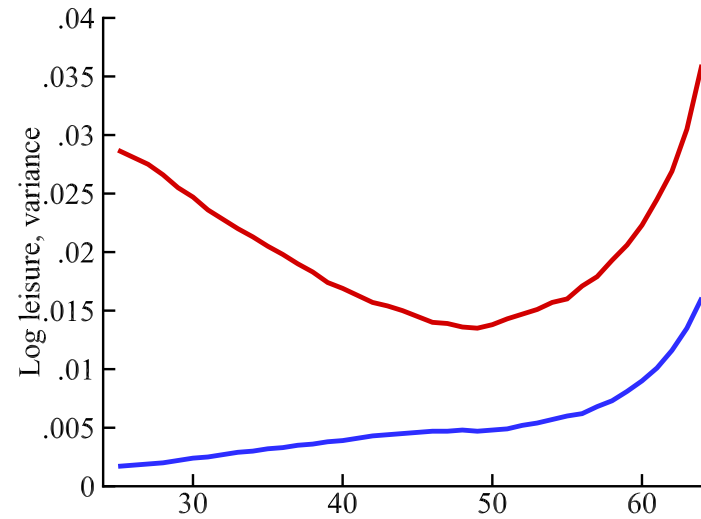
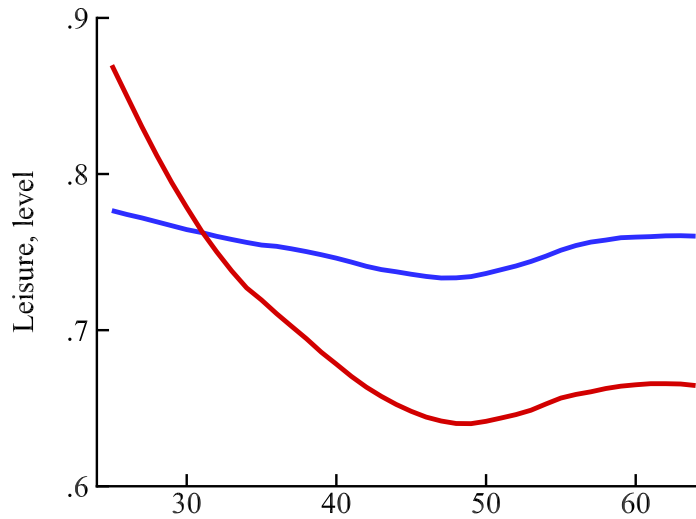
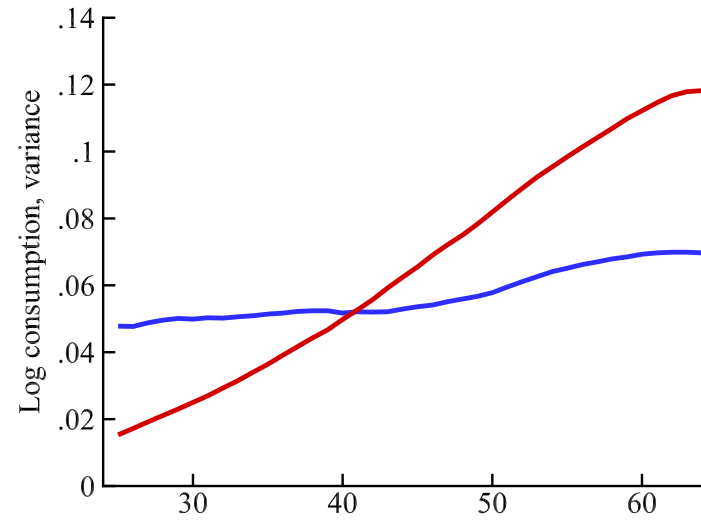
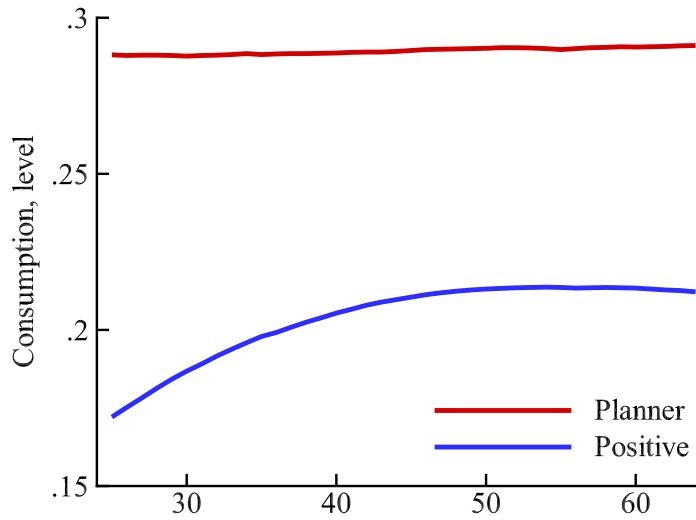


# A Look Under the Hood: Group LL



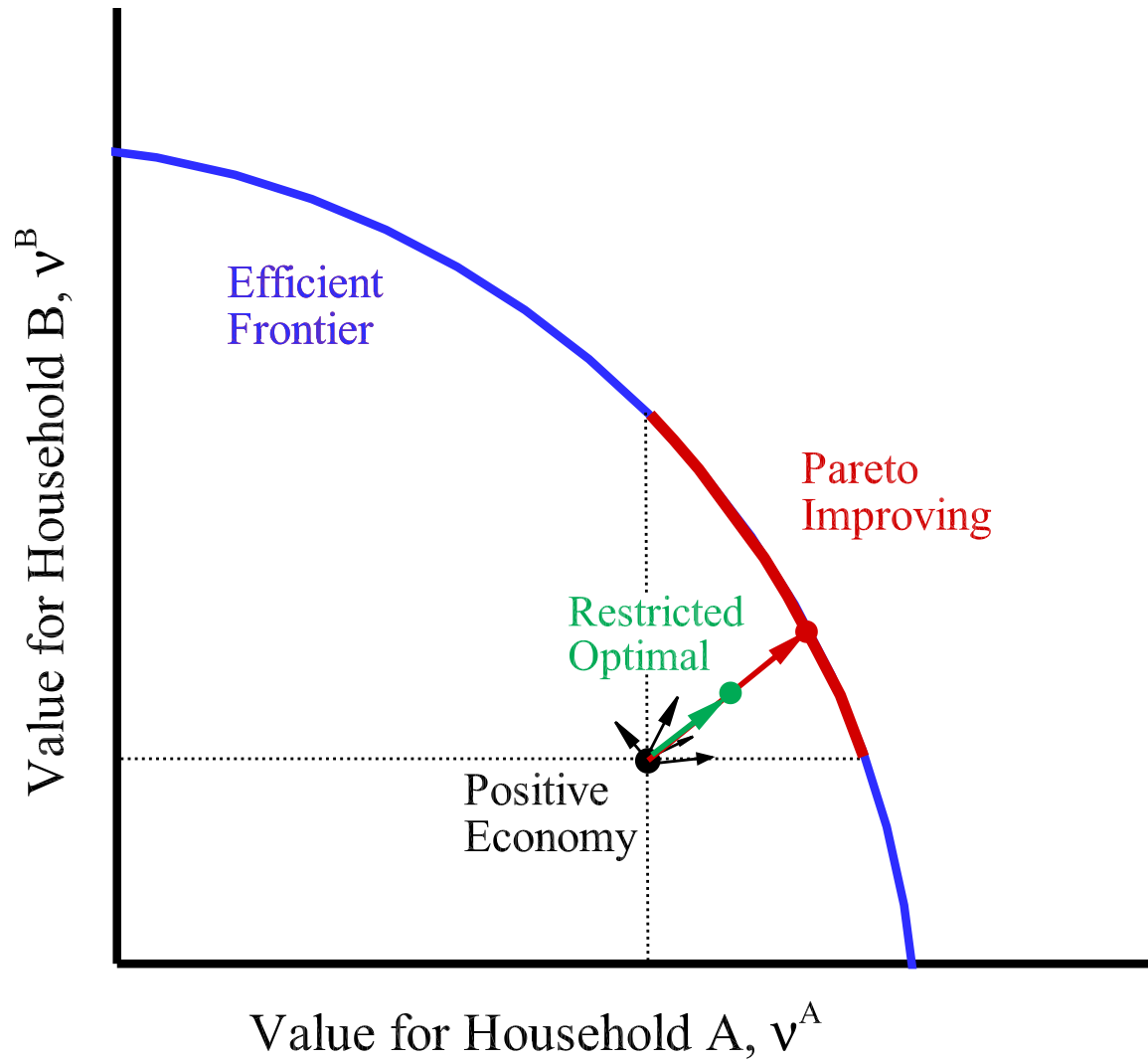


# A Look Under the Hood: Group LL





# Informing Counterfactuals (●)







## Informing Counterfactuals (●)

- Main source of gains:
  - Increased consumption early in life
- Suggests large gains to early-life transfer
  - Without it, found restricted gains of 5%
  - With it, found restricted gains of 7%

out of total of 21%

*Note:* Estimates of restricted gains still tentative



# Summary

- Ultimate goals of project:
  - Estimates of gains for efficient reform
  - Identification of sources of gains
  - Ideas for new policy instruments
  - Prototype for future analyses
  
- Stay tuned...



# Mathematical Appendix



## Positive Economy: Household

$$v_j(a, \epsilon; \Omega) = \max_{c, n, a'} \{U(c, \ell) + \beta E[v_{j+1}(a', \epsilon'; \Omega) | \epsilon]\}$$

$$\text{s.t. } a' = (1 + r)a - T_a(ra) + w\epsilon n - T_n(j, w\epsilon n) - (1 + \tau_c)c$$

where

$j$  = age

$a$  = financial assets

$\epsilon$  = productivity shock

$\Omega$  = factor prices and tax policies

$c$  = consumption

$n$  = labor supply ( $n + \ell = 1$ )



# Planner Problem for a Household



# Planner Problem for a Household

Max present value of resources



# Planner Problem for a Household

$$\Pi_j(V, \tilde{V}, \epsilon) \equiv \max_{\epsilon_i} \sum \pi_j(\epsilon_i | \epsilon) [w\epsilon_i n_j(\epsilon_i) - c_j(\epsilon_i) + \Pi_{j+1}(V_j(\epsilon_i), \tilde{V}_j(\epsilon_{i+1}), \epsilon_i) / R]$$



# Planner Problem for a Household

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s.t. Local downward incentive constraints





## Planner Problem for a Household

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$$\begin{aligned} \text{s.t. } & U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i) \\ & \geq U(c_j(\epsilon_{i-1}), \ell_j^+(\epsilon_{i-1})) + \beta \tilde{V}_j(\epsilon_i), \quad i \geq 2 \end{aligned}$$

$$\text{where } \ell_j^+(\epsilon_{i-1}) = 1 - n_j(\epsilon_{i-1})\epsilon_{i-1}/\epsilon_i$$



## Planner Problem for a Household

$$\begin{aligned} \Pi_j(V, \tilde{V}, \epsilon) &\equiv \max_{\epsilon_i} \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [w\epsilon_i n_j(\epsilon_i) - c_j(\epsilon_i) \\ &\quad + \Pi_{j+1}(V_j(\epsilon_i), \tilde{V}_j(\epsilon_{i+1}), \epsilon_i) / R] \\ \text{s.t. } &U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i) \\ &\geq U(c_j(\epsilon_{i-1}), \ell_j^+(\epsilon_{i-1})) + \beta \tilde{V}_j(\epsilon_i), \quad i \geq 2 \end{aligned}$$

Deliver at least the promised value



# Planner Problem for a Household

$$\Pi_j(V, \tilde{V}, \epsilon) \equiv \max_{\epsilon_i} \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [w\epsilon_i n_j(\epsilon_i) - c_j(\epsilon_i) + \Pi_{j+1}(V_j(\epsilon_i), \tilde{V}_j(\epsilon_{i+1}), \epsilon_i) / R]$$

$$\text{s.t. } U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i) \geq U(c_j(\epsilon_{i-1}), \ell_j^+(\epsilon_{i-1})) + \beta \tilde{V}_j(\epsilon_i), \quad i \geq 2$$

$$V \leq \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i)]$$



## Planner Problem for a Household

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Deliver no more than the threat value



# Planner Problem for a Household

$$\Pi_j(V, \tilde{V}, \epsilon) \equiv \max_{\epsilon_i} \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [w\epsilon_i n_j(\epsilon_i) - c_j(\epsilon_i) + \Pi_{j+1}(V_j(\epsilon_i), \tilde{V}_j(\epsilon_{i+1}), \epsilon_i) / R]$$

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$$V \leq \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i)]$$

$$\tilde{V} \geq \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon^+) [U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i)]$$



# Planner Problem for Future Generation ( $j = 1$ )

$$\Pi_j(V, -, \epsilon) \equiv \max_{\epsilon_i} \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [w\epsilon_i n_j(\epsilon_i) - c_j(\epsilon_i) + \Pi_{j+1}(V_j(\epsilon_i), \tilde{V}_j(\epsilon_{i+1}), \epsilon_i) / R]$$

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No threat value



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$$V \leq \sum_{\epsilon_i} \pi_j(\epsilon_i | \epsilon) [U(c_j(\epsilon_i), \ell_j(\epsilon_i)) + \beta V_j(\epsilon_i)]$$

Replace arbitrary  $V$  with  $\vartheta(\epsilon_0) + \vartheta_\Delta$