



# OPENNESS, TECHNOLOGY CAPITAL, AND DEVELOPMENT

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## TECHNOLOGY CAPITAL

- Is accumulated know-how from investments in
  - R&D
  - Brands
  - Organization know-how

which can be used in as many *locations* as firms choose



## OUR THESIS

- Technology capital is critical to
  - Assessing gains from opening to FDI
  - Predicting current account flows/balances



## NEW MODEL OF FDI

- Countries are measures of locations
- Technology capital can be used in multiple locations
- Doesn't require monopoly rents to finance innovations



## NEW AVENUE FOR GAINS FROM FDI

- Opening implies bigger aggregate production sets
- In our model, gains arise
  - Without increasing returns
  - Without traditional factor endowment differences
  - Even with symmetric countries



## MAIN FINDINGS

- Gains from opening to FDI are large
- Current account “puzzles” are not so puzzling



# THEORY





## CLOSED-ECONOMY AGGREGATE OUTPUT

$$Y = A(NM)^\phi Z^{1-\phi}$$

$M$  = units of *technology capital*

$Z$  = composite of other factors,  $K^\alpha L^{1-\alpha}$

$N$  = number of production *locations*

$A$  = the technology parameter

$\phi$  = the income share parameter

which is the result of maximizing plant-level output





# A MICRO FOUNDATION FOR AGGREGATE FUNCTION

- $n \in \{1, \dots, N\}, m \in \{1, \dots, M\}$

$$F(N, M, Z) = \max_{z_{nm}} \sum_{n,m} g(z_{nm})$$

$$\text{subject to } \sum_{n,m} z_{nm} \leq Z$$

We assume  $g(z) = Az^{1-\phi}$ , increasing and strictly concave



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$\Rightarrow$  organizational span of control limits



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$\Rightarrow$  optimal to split  $Z$  evenly across location-technologies



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$$\text{subject to } \sum_{n,m} z_{nm} \leq Z$$

$$\Rightarrow F(N, M, Z) = NMg(Z/NM) = A(NM)^\phi Z^{1-\phi}$$



# A MICRO FOUNDATION FOR AGGREGATE FUNCTION

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$$F(N, M, Z) = \max_{z_{nm}} \sum_{n,m} g(z_{nm})$$

$$\text{subject to } \sum_{n,m} z_{nm} \leq Z$$

$$\Rightarrow F(N, \lambda M, \lambda Z) = \lambda F(N, M, Z)$$



## PRODUCTION IN OPEN ECONOMY

- The degree of openness of country  $i$  is  $\sigma_i \in [0, 1]$
- Aggregate output in  $i$  is

$$\max_{z_d, z_f} M_i N_i A_i z_d^{1-\phi} + \sigma_i \sum_{j \neq i} M_j N_i A_i z_f^{1-\phi}$$

$$\text{subject to } M_i N_i z_d + \sum_{j \neq i} M_j N_i z_f \leq Z_i$$

$d, f$  indexes allocations to domestic and foreign operations



## PRODUCTION IN OPEN ECONOMY

- Aggregate output in  $i$  is

$$Y_i = A_i N_i^\phi (M_i + \omega_i \sum_{j \neq i} M_j)^\phi Z_i^{1-\phi}$$

where

$$Z_i = K_i^\alpha L_i^{1-\alpha}$$

$$\omega_i = \sigma_i^{\frac{1}{\phi}}$$

- Alternative interpretation of openness: fraction of  $M_j$  let in



## PRODUCTION IN OPEN ECONOMY

- Aggregate output in  $i$  is

$$Y_i = A_i N_i^\phi (M_i + \omega_i \sum_{j \neq i} M_j)^\phi Z_i^{1-\phi}$$

- Key result provided  $\omega_i > 0$ :

Each  $i$  has constant returns, but summing over  $i$  results in a *bigger* aggregate production set.





## PRODUCTION IN OPEN ECONOMY

- Aggregate output in  $i$  is

$$Y_i = A_i N_i^\phi (M_i + \omega_i \sum_{j \neq i} M_j)^\phi Z_i^{1-\phi}$$

- Key result:

It is *as if* there were increasing returns,  
when in fact there are none.



## PRODUCTION IN OPEN ECONOMY

- Aggregate output in  $i$  is

$$Y_i = A_i N_i^\phi (M_i + \omega_i \sum_{j \neq i} M_j)^\phi Z_i^{1-\phi}$$

- Key result:

We partially endogenize measured TFP since locations and technology capital affect measured TFP.



## ASSESSING GAINS TO OPENNESS

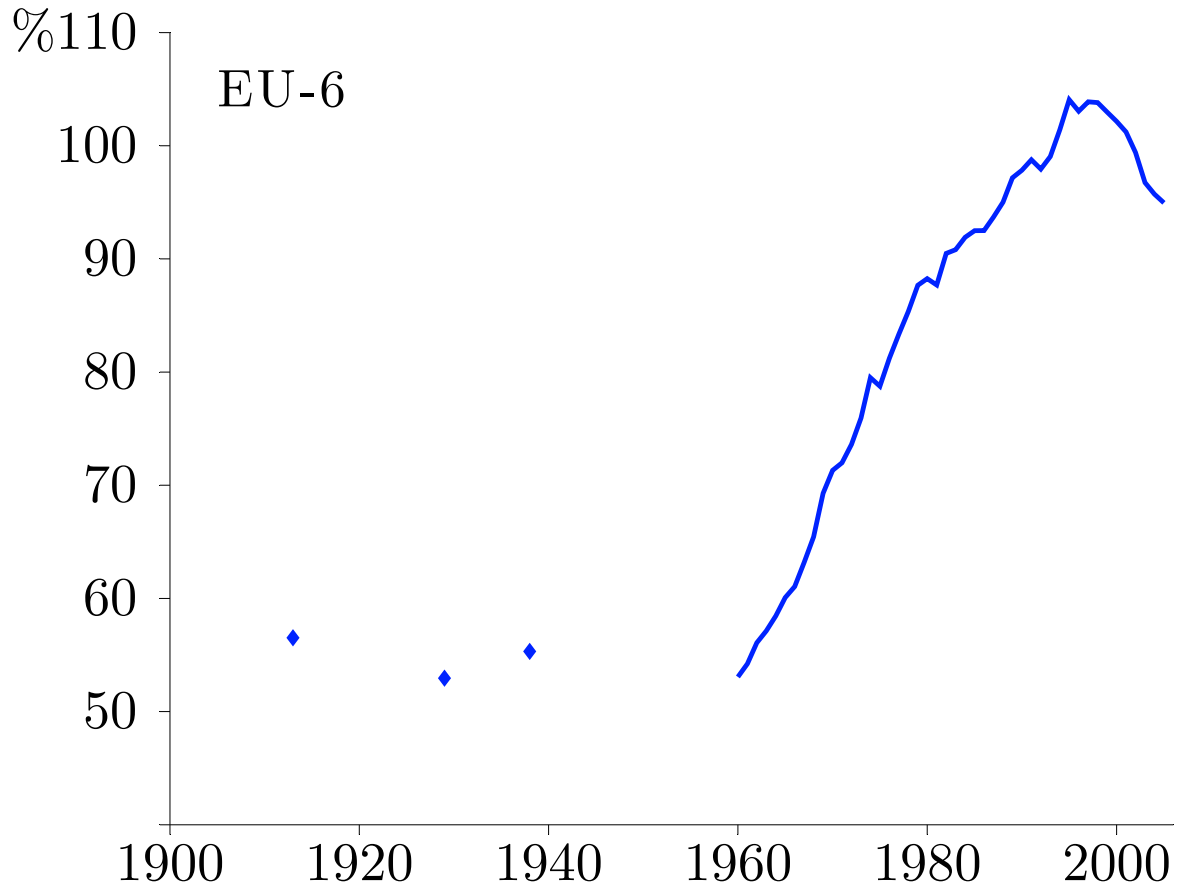


## GAINS TO OPENING TO FDI

- Empirical evidence:
  - Mixed results in regressions of growth on FDI
  - But, huge successes of economic unions (eg, EU)



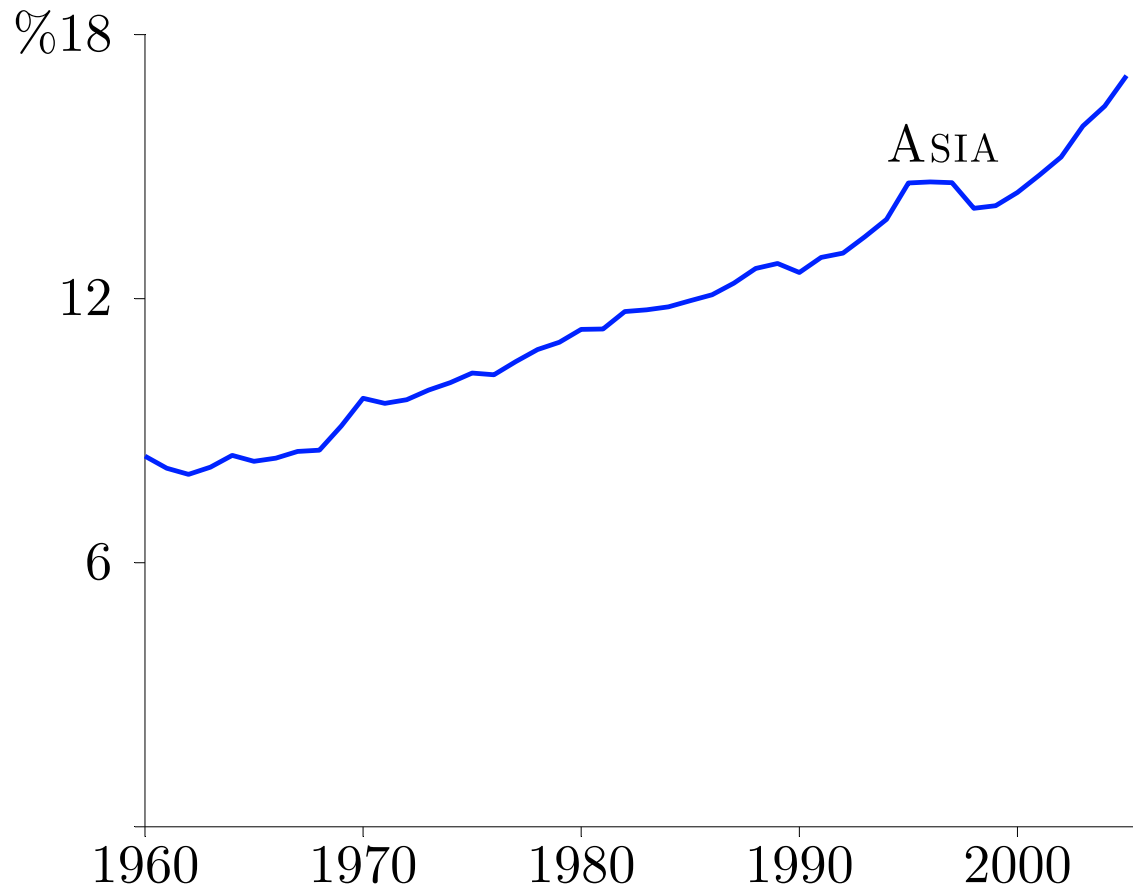
# WHY DID THE EU-6 CATCH UP?



EU-6 LABOR PRODUCTIVITY AS % OF US



# WHY IS ASIA STARTING TO CATCH UP?

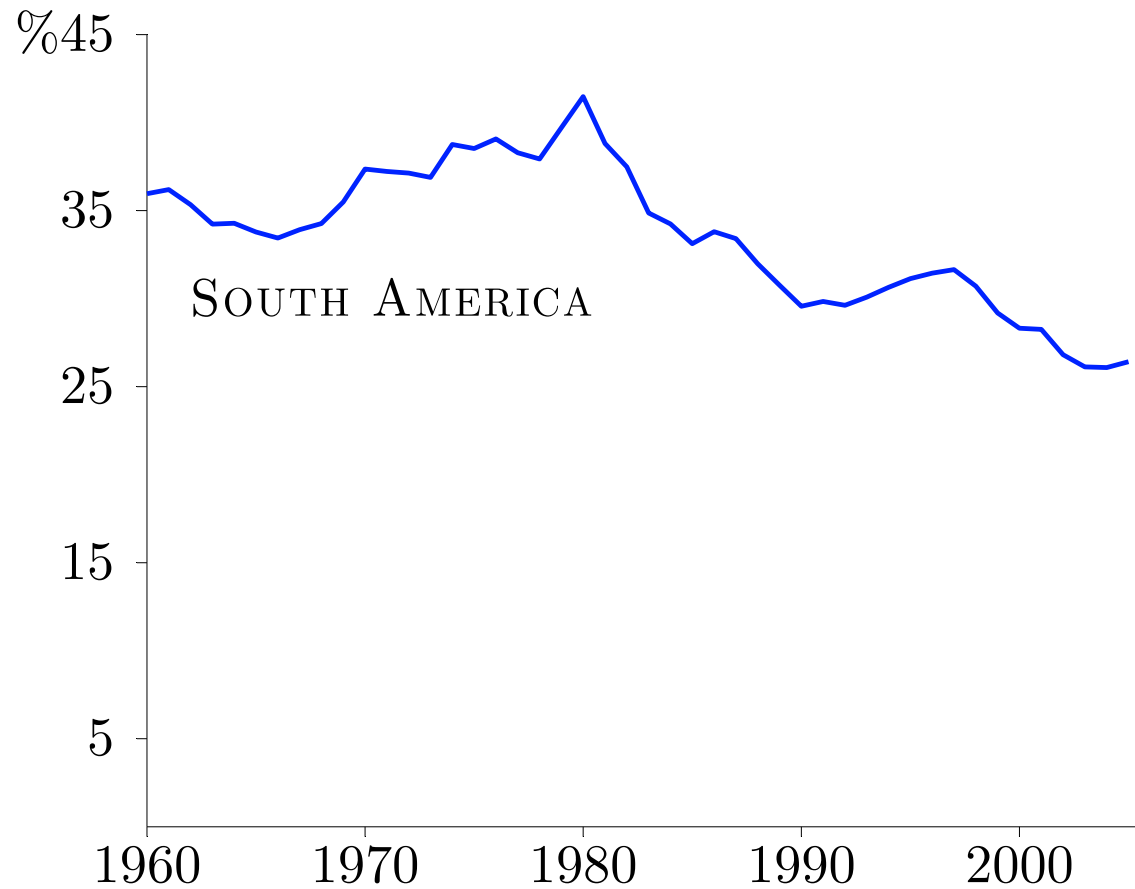


ASIAN LABOR PRODUCTIVITY AS % OF US





# WHILE SOUTH AMERICA IS LOSING GROUND?



SOUTH AMERICAN LABOR PRODUCTIVITY AS % OF US





## QUESTIONS

- Why did the EU-6 catch up?
- Why is Asia starting to catch up?
- Why is South America losing ground?
- And, specifically, what role does FDI play?





## WHAT ROLE DOES FDI PLAY?

- Answer depends on countries' openness policy and size
- Definition:  $\text{Size} = \mathcal{A}_i N_i$

$\mathcal{A}_i$  is level of technology,  $A_i^{\frac{1}{1-\alpha(1-\phi)}}$

$N_i$  is number of production locations



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$N_i$  is number of production locations

$\propto$  population in  $i$



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$N_i$  is number of production locations

$\Rightarrow$  expanding markets requires more consumers



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$N_i$  is number of production locations

$\Rightarrow$  Canada is like Taiwan, not China



# STEADY STATE ANALYSIS



## A STEADY STATE

- Common world interest rate determined by preferences
- Common  $K/Y$  ratio determined by interest rate
- **Key result:** Some  $M_i$  may be zero



## KEY EQUILIBRIUM CONDITIONS

- $K_i/Y_i$  same across  $i$

$$\Rightarrow Y_i = \psi \mathcal{A}_i N_i (M_i + \omega_i \sum_{j \neq i} M_j)^{\frac{\phi}{1-\alpha(1-\phi)}}$$

- Combined with

$$\sum_j \partial Y_j / \partial M_i \leq \rho + \delta_m, \quad = \text{if } M_i > 0$$

$\Rightarrow$  System for which we apply Kakutani theorem



# THREE LESSONS FROM STEADY STATE ANALYSIS





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2. A union of small countries is like a large country



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3. Countries gain when unilaterally opening



## THREE LESSONS FROM STEADY STATE ANALYSIS

1. There is an advantage to size if world closed
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Let's consider an example that illustrates 3 lessons ...



EXAMPLE:  $I = 2$ , SYMMETRIC  $\omega$

- Country 1 is larger,  $\mathcal{A}_1 N_1 > \mathcal{A}_2 N_2$
- Key equilibrium conditions imply a  $\omega^*$  such that:

Case 1:  $M_1 > 0, M_2 > 0$  if  $\omega < \omega^*$

Case 2:  $M_1 > 0, M_2 = 0$  if  $\omega > \omega^*$



## LESSON 1: SIZE ADVANTAGE ( $\omega < \omega^*$ )

- Country 1 is larger,  $\mathcal{A}_1 N_1 > \mathcal{A}_2 N_2$
- If  $\omega < \omega^*$ , then  $M_1, M_2 > 0$  and

$$\frac{Y_i}{N_i} \propto (M_i + \omega M_{-i})^{\frac{\phi}{1-\alpha(1-\phi)}} \mathcal{A}_i$$

What matters is effective technology capital,  $M_i + \omega M_{-i}$



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$$\frac{Y_i}{N_i} \propto (M_i + \omega M_{-i})^{\frac{\phi}{1-\alpha(1-\phi)}} \mathcal{A}_i$$

$$\text{and } \frac{Y_i}{N_i} \propto [(1 + \omega)\mathcal{A}_i N_i]^{\frac{\phi}{(1-\alpha)(1-\phi)}} \mathcal{A}_i$$

Which is proportional to size



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$$\text{and } \frac{Y_i}{N_i} \propto [(1 + \omega) \mathcal{A}_i N_i]^{\frac{\phi}{(1-\alpha)(1-\phi)}} \mathcal{A}_i$$

Implying an advantage to size when  $\omega$  small





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$$\rightarrow \mathcal{A}_i \text{ as } \phi \rightarrow 0$$

As  $\phi \rightarrow 0$ , back to standard theory



## LESSON 1: SIZE ADVANTAGE ( $\omega > \omega^*$ )

- Country 1 is larger,  $\mathcal{A}_1 N_1 > \mathcal{A}_2 N_2$
- If  $\omega > \omega^*$ , then  $M_2 = 0$  and

$$\frac{Y_1}{N_1} \propto (Y_1 + Y_2)^{\frac{\phi}{1-\alpha(1-\phi)}} \mathcal{A}_1$$

$$\frac{Y_2}{N_2} \propto (\omega(Y_1 + Y_2))^{\frac{\phi}{1-\alpha(1-\phi)}} \mathcal{A}_2$$

When  $\omega > \omega^*$ , small country uses  $M_1$



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Implying a disappearing advantage as  $\omega \rightarrow 1$



## LESSON 1: SIZE ADVANTAGE ( $\omega > \omega^*$ )

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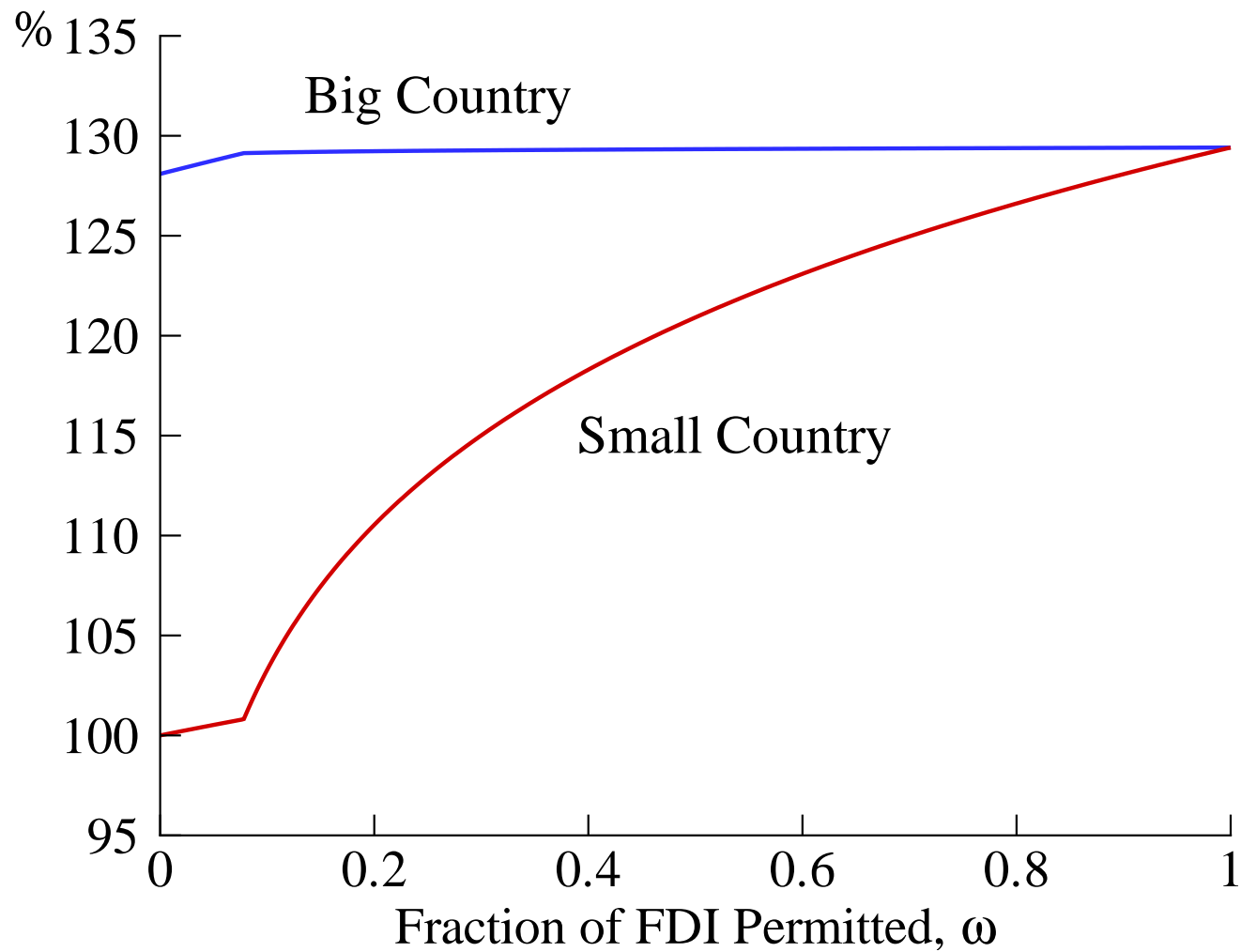
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As  $\phi \rightarrow 0$ , back to standard theory



# PRODUCTIVITIES VS. $\omega$ , $\mathcal{A}_1 N_1 = 10\mathcal{A}_2 N_2$





## LESSON 2: GAIN FROM FORMING UNIONS

- $I$  = number of equal-sized countries forming union
- Then, factor gain in productivity  $y$  for union is

$$y(I)/y(1) = I^{\frac{\phi}{(1-\alpha)(1-\phi)}}$$

- A union of small countries is like a large country



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- How large are the potential gains?



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$$y(I)/y(1) = I^{\frac{\phi}{(1-\alpha)(1-\phi)}}$$

- If  $\alpha = .3$ ,  $\phi = .07$ , then

$$\text{Gain} = 28\% \quad \text{if } I = 10$$

$$\text{Gain} = 64\% \quad \text{if } I = 100$$





## LESSON 3: GAIN FROM UNILATERALLY OPENING

- $I$  = number of equal-sized countries remaining closed
- Then, factor gain in productivity of  $I + 1$ st opening is

$$y_o/y_c = I^{\frac{\phi}{1-\alpha(1-\phi)}}$$

- Countries gain when unilaterally opening



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- Then, factor gain in productivity of  $I + 1$ st opening is

$$y_o/y_c = I^{\frac{\phi}{1-\alpha(1-\phi)}}$$

- If  $\alpha = .3$ ,  $\phi = .07$ , then

$$\text{Gain} = 25\% \quad \text{if } I = 10$$

$$\text{Gain} = 56\% \quad \text{if } I = 100$$



## BOTTOM LINE

- Gains to opening are large if  $\phi$  not small
- To determine how large, need to know  $\phi$



## USING US ACCOUNTS TO ESTIMATE $\phi$

- If  $\phi$  sizable, gains to opening are large
- In “Technology Capital and the US Current Account”
  - Chose  $\phi$ , size, openness to match US
    - International accounts
    - National accounts
  - Needed  $\phi = .07$  for consistency with accounts



# TECHNOLOGY CAPITAL AND THE US CURRENT ACCOUNT

- Households choose:

Consumption, hours, domestic & foreign equity and debt

- Multinationals choose:

Locations, labor, and tangible and intangible capitals

- No asset or goods market frictions

⇒ Generate domestic and current accounts for the model



# TECHNOLOGY CAPITAL AND THE US CURRENT ACCOUNT

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- Multinationals choose:

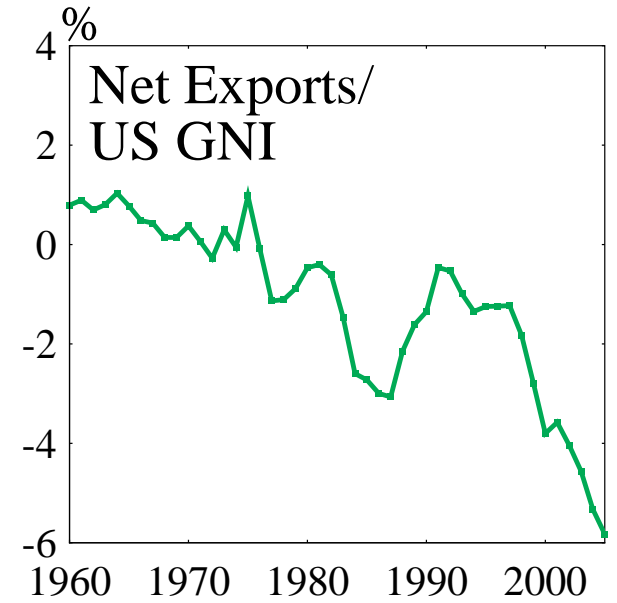
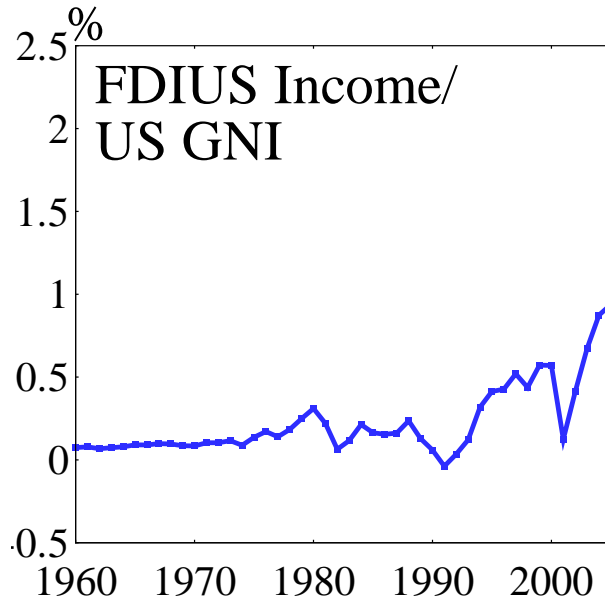
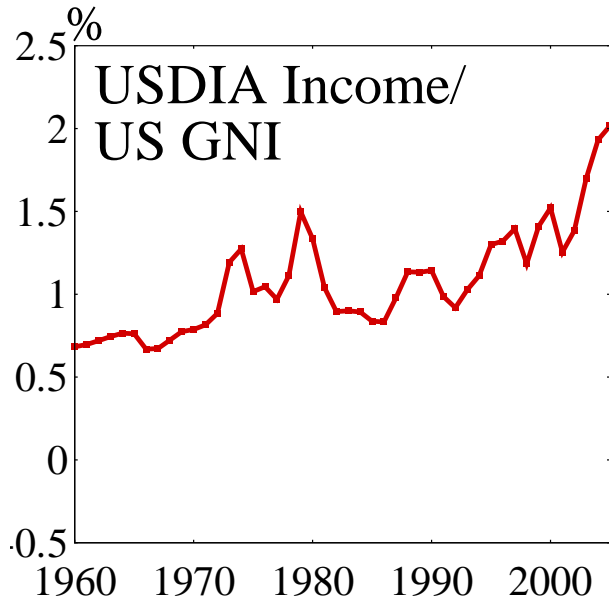
Locations, labor, and tangible and intangible capitals

- No asset or goods market frictions

⇒ Can directly compare model and US accounts



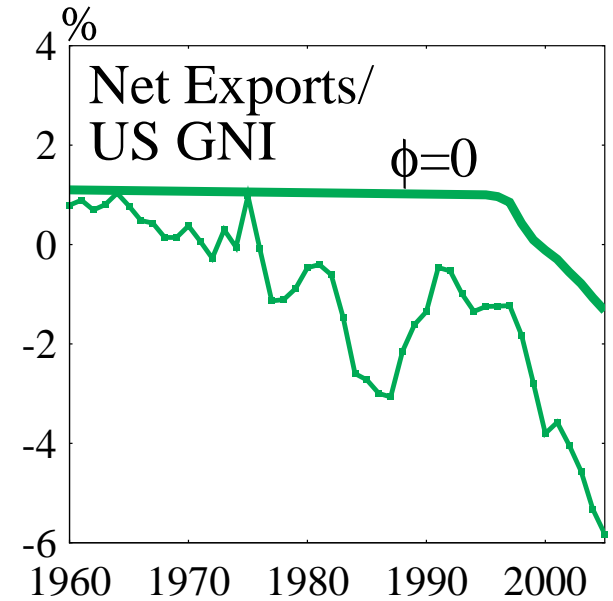
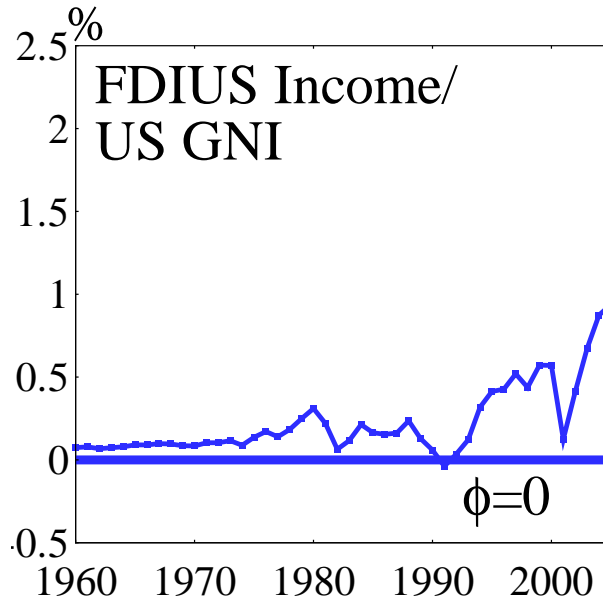
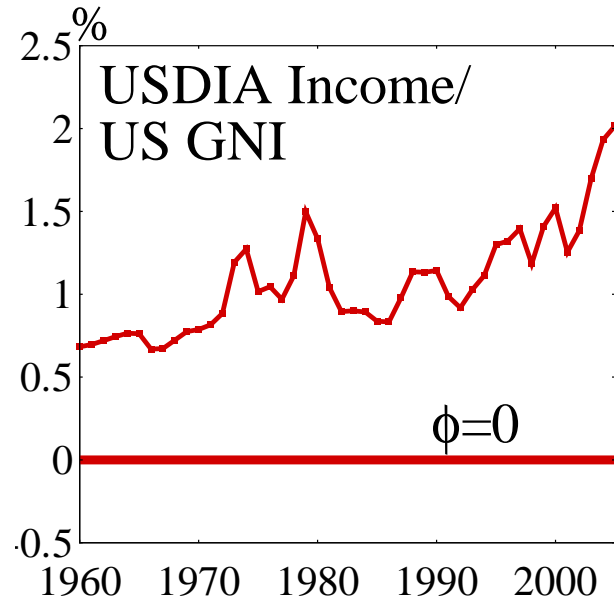
# FDI INCOMES AND TRADE BALANCE







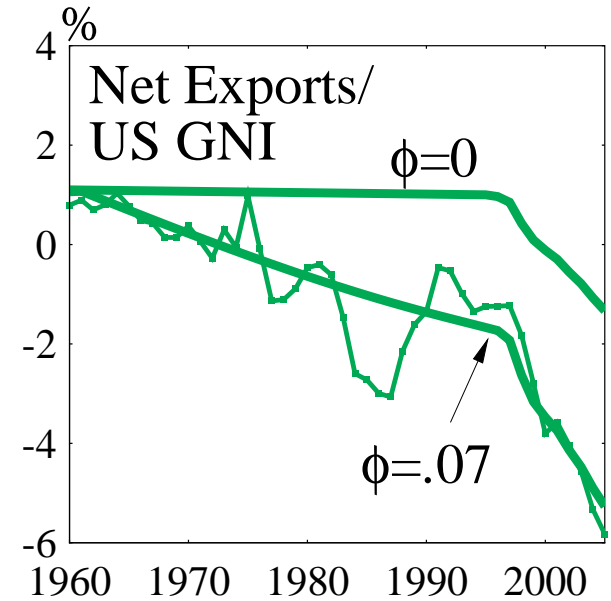
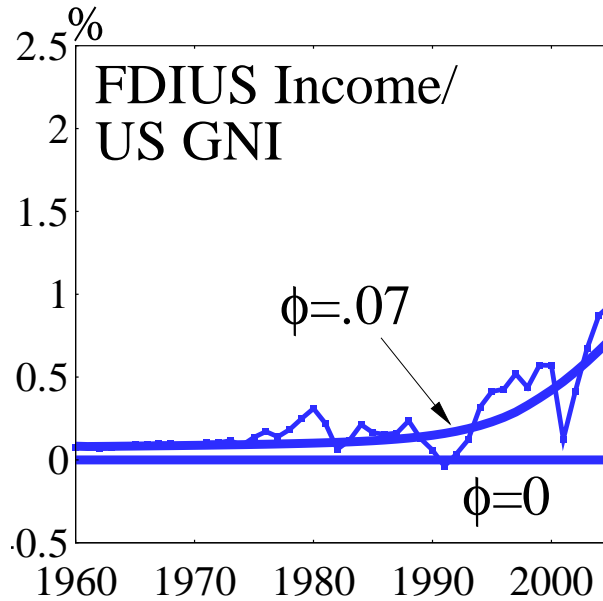
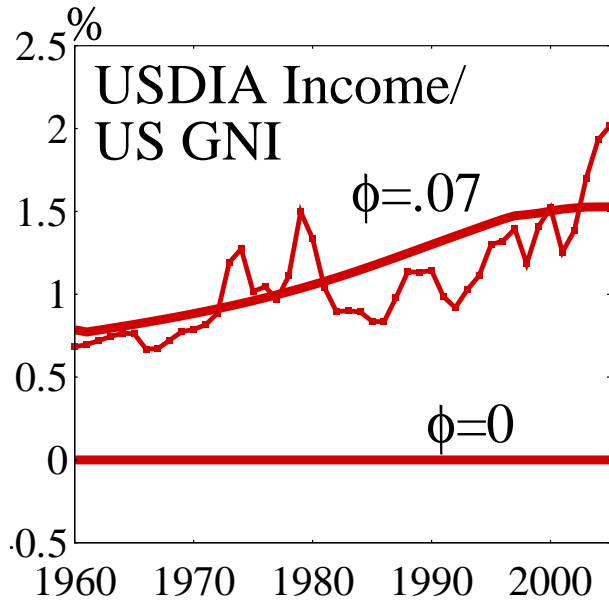
# FDI INCOMES AND TRADE BALANCE, $\phi = 0$



No technology capital case



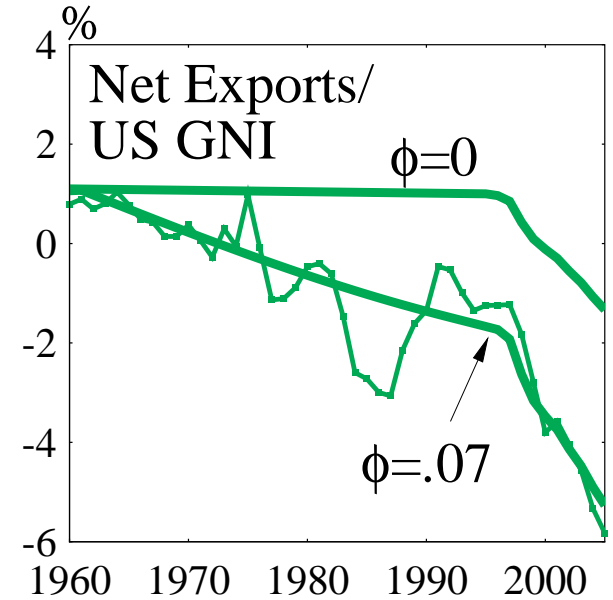
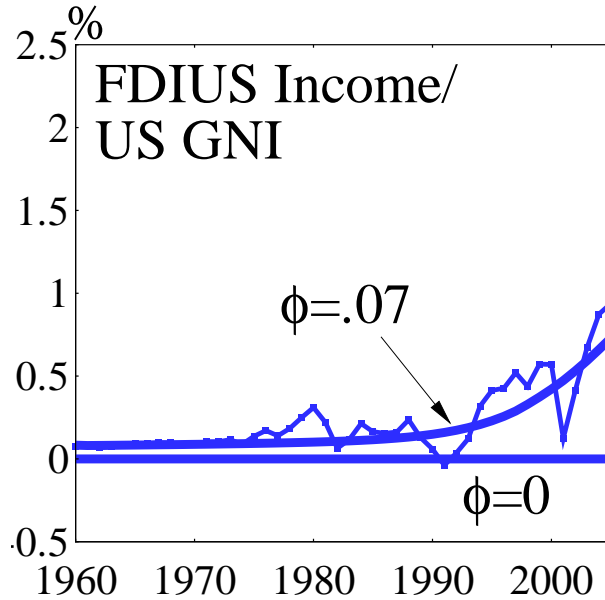
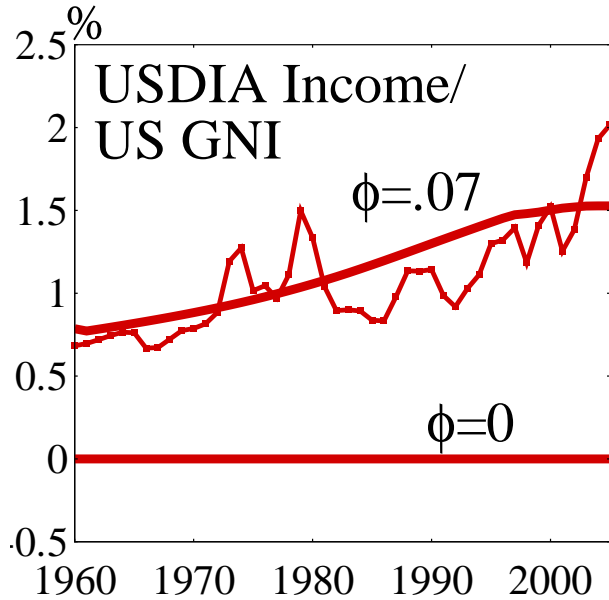
# FDI INCOMES AND TRADE BALANCE, $\phi = .07$



Increase  $\phi$  to fit trends in data



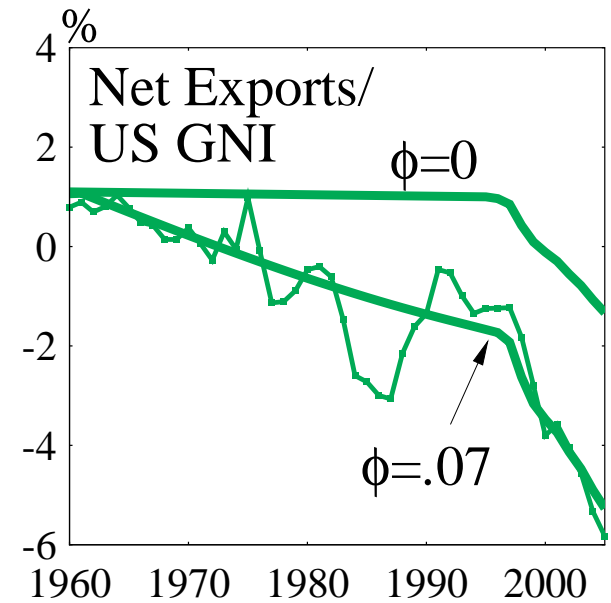
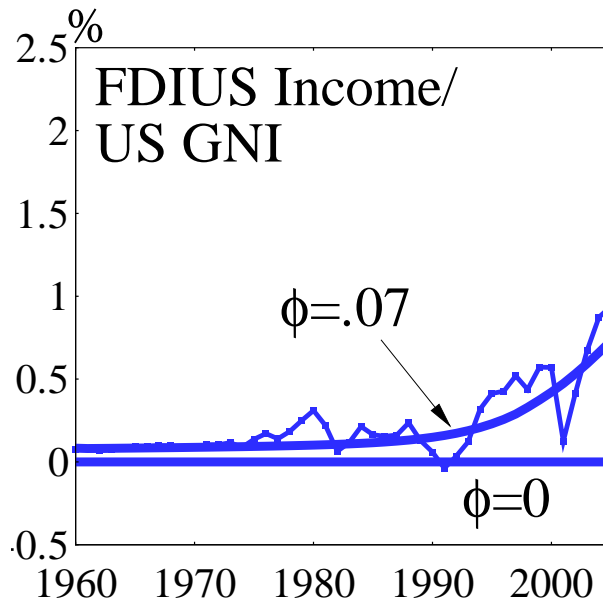
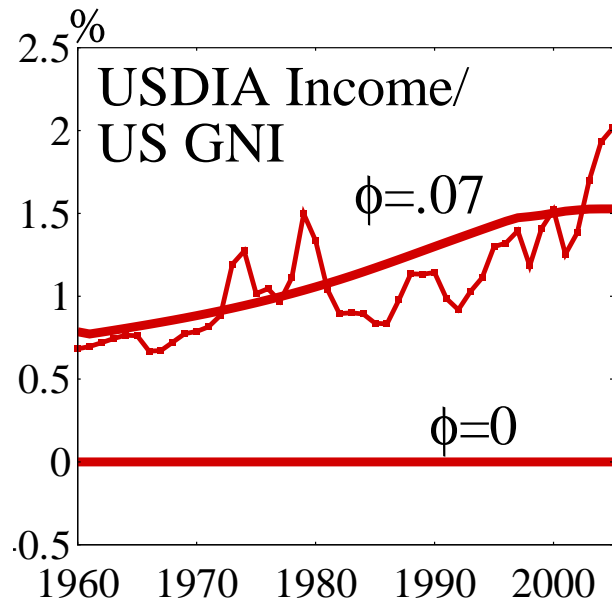
# FDI INCOMES AND TRADE BALANCE, $\phi = .07$



International data consistent with  $\phi = .07$



# FDI INCOMES AND TRADE BALANCE, $\phi = .07$



Bottom line: gains from opening to FDI are large



## INTUITION FOR LARGE DECLINE IN NET EXPORTS

- Let  $u=US$ ,  $r=ROW$
- Net exports relative to size for US and ROW:

$$\frac{NX_u}{\mathcal{A}_u N_u} = \frac{Y_u - X_{m,u} - X_{k,u} - C_u}{\mathcal{A}_u N_u} \quad (1)$$

$$\frac{-NX_u}{\mathcal{A}_r N_r} = \frac{Y_r - X_{m,r} - X_{k,r} - C_r}{\mathcal{A}_r N_r} \quad (2)$$

where  $X_m, X_k$  are investments in  $M$  and  $K$

- Subtract (2) from (1)



## INTUITION FOR LARGE DECLINE IN NET EXPORTS

- If change in size due to change in population, then

$$\begin{aligned}
 \left( \frac{1}{A_u N_u} + \frac{1}{A_r N_r} \right) NX_u &= \underbrace{\left( \frac{X_{k,u}}{A_u N_u} - \frac{X_{k,r}}{A_r N_r} \right)}_{\text{Equates } K/Y\text{'s}} + \underbrace{\left( \frac{C_u}{A_u N_u} - \frac{C_r}{A_r N_r} \right)}_{=0} \\
 &+ \underbrace{\left( \frac{X_{m,u}}{A_u N_u} - \frac{X_{m,r}}{A_r N_r} \right)}_{\substack{=0 \text{ if } \phi=0 \\ \text{amplifies } X_k \text{ term if } \phi>0}} + \underbrace{\left( \frac{Y_u}{A_u N_u} - \frac{Y_r}{A_r N_r} \right)}_{\substack{=0 \text{ if } \phi=0 \\ \text{varies with size if } \phi>0}}
 \end{aligned}$$

- Implies large decline in  $NX_u$  and reversal



## CURRENT ACCOUNT PUZZLES NOT SO PUZZLING

- With technology capital included, predict
  - Large decline in net exports share
  - Large rise in consumption share
  - Large gap between USDIA and FDIUS returns



## WHAT IMPLICATIONS FOR GROWTH REGRESSIONS?

- Mixed results in regressions of growth on FDI
- Not surprising in light of our theory which
  - Predicts level effects rather than growth effects
  - Points to FDI *incomes*, not investments as key variables
  - Requires knowledge of openness policies over time





AN EXAMPLE TRANSITION TO ILLUSTRATE THE POINT



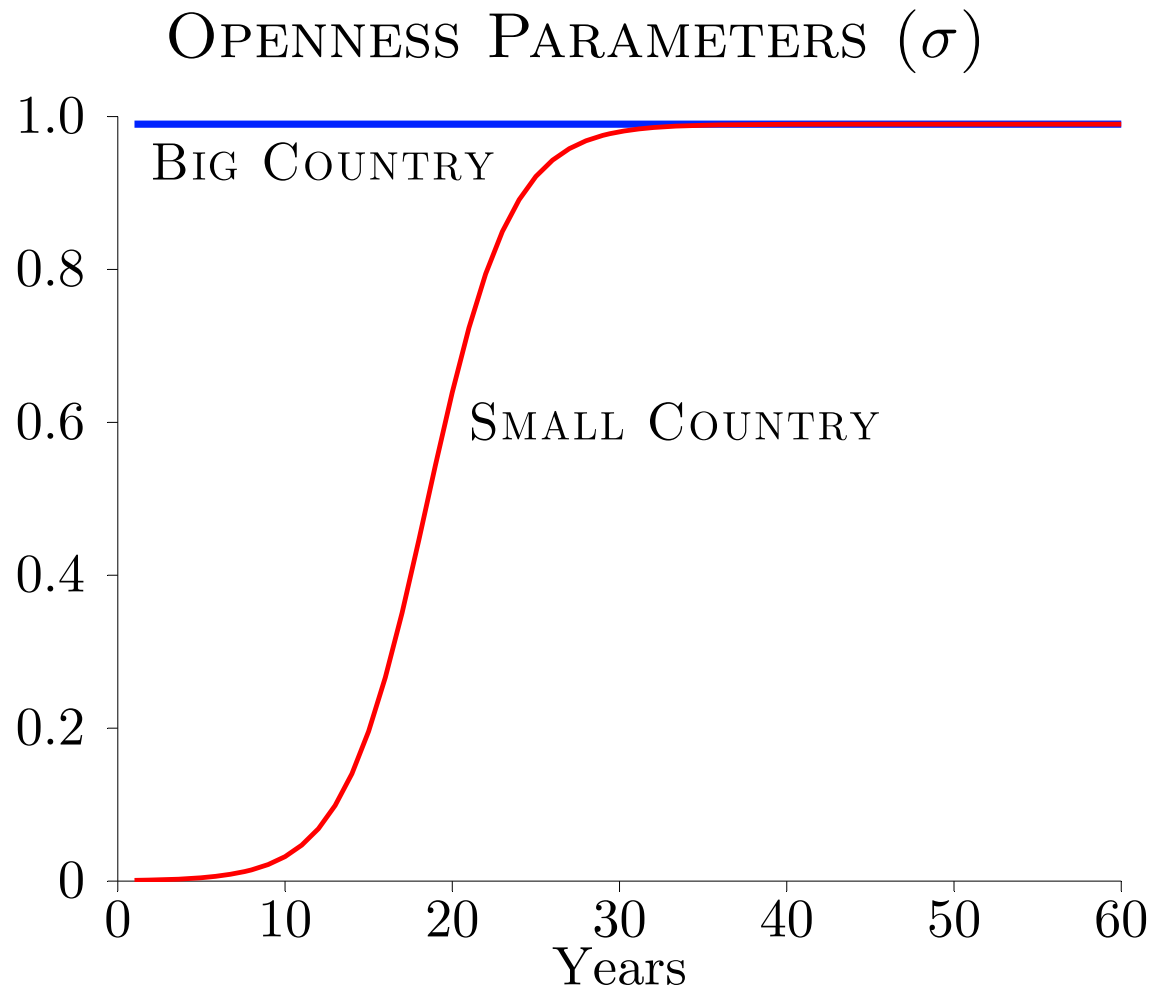


## AN EXAMPLE TRANSITION

- Two countries, closed at date 0
- In date 1,
  - Big country ( $\mathcal{AN} = 10$ ) opens up rapidly
  - Small country ( $\mathcal{AN} = 1$ ) opens up gradually

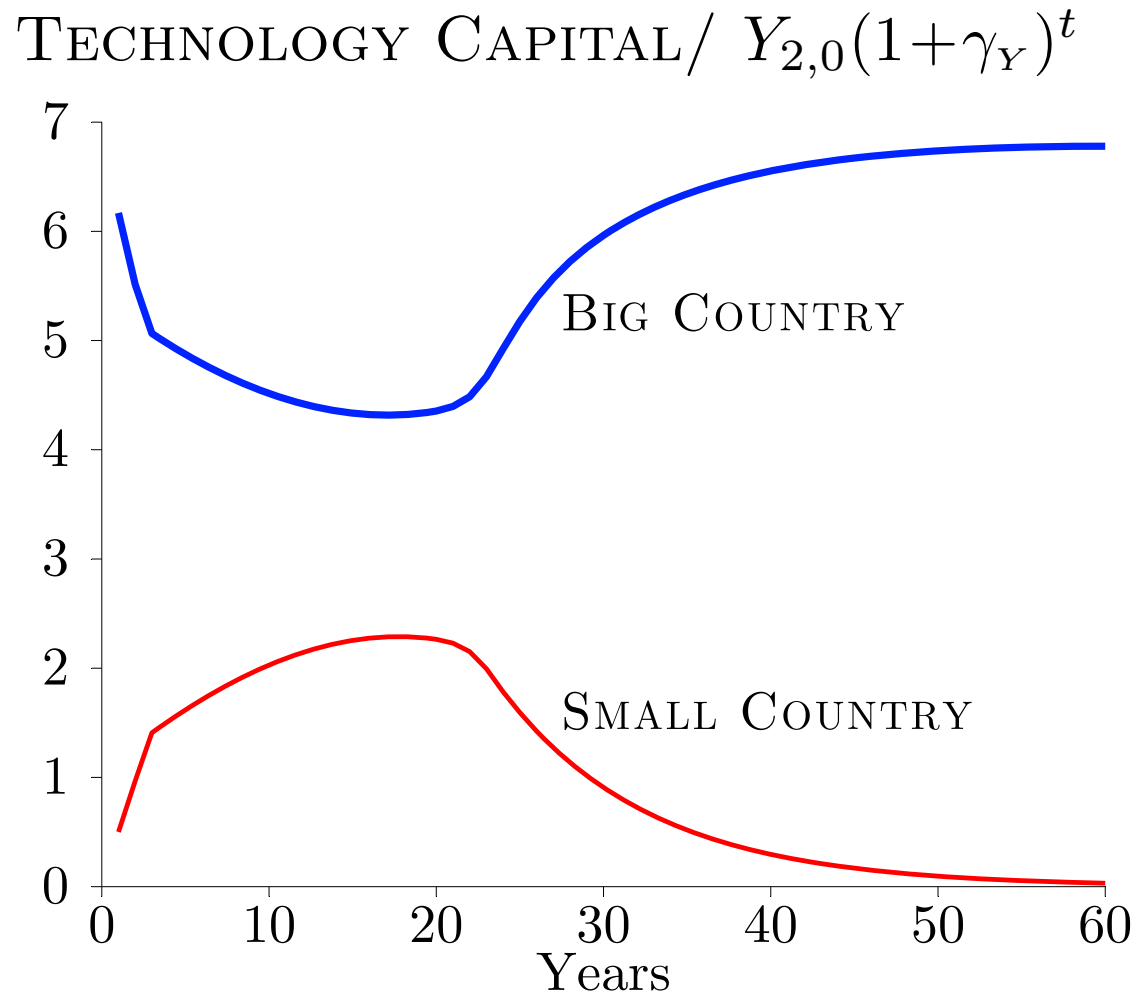


# SMALL COUNTRY OPENS GRADUALLY





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## SMALL COUNTRY OPENS GRADUALLY

- Initially, small country
  - Takes advantage of new markets in big country
  - Invests **more** in technology capital
  - Experiences a **drop** in measured productivity
  - **Scares** observers at the IMF
- Eventually exploits big country's technology capital stock



## SUMMARY

- Paper extends neoclassical growth model by adding
  - Locations
  - Technology capital
- These additions are critical in assessing
  - Gains from opening to FDI
  - US current account flows/balances



## APPENDIX:

A DECENTRALIZATION TO MATCH TO BEA ACCOUNTS



## HOUSEHOLDS IN $i$ SOLVE

$$\max \sum_t \beta^t U \left( \frac{C_{it}}{N_{it}}, \frac{L_{it}}{N_{it}} \right) N_{it}$$

subject to budget constraint

$$\begin{aligned} \sum_t p_t \left[ (1 + \tau_{c,it}) C_{it} + \sum_j V_t^j (S_{i,t+1}^j - S_{it}^j) + B_{i,t+1} - B_{it} \right] \\ \leq \sum_t p_t \left[ (1 - \tau_{l,it}) W_{it} L_{it} + (1 - \tau_{d,t}) \sum_j S_{it}^j D_t^j + r_{b,t} B_{it} + \kappa_{it} \right] \end{aligned}$$

$S_i^j$  = equity shares of companies in  $j$

$B_i$  = foreign debt





# MULTINATIONALS INCORPORATED IN COUNTRY $j$ SOLVE

$$\max \sum_t p_t (1 - \tau_{d,t}) D_t^j$$

where dividends  $D_t^j$  satisfy

$$\begin{aligned} D_t^j + \underbrace{\sum_i K_{T,i,t+1}^j - K_{T,it}^j}_{\text{Reported reinvested earnings}} \\ = \underbrace{\sum_i \{(1 - \tau_{p,it}) (Y_{it}^j - W_{it} L_{it}^j - \delta_T K_{T,it}^j - X_{I,it}^j - \chi_i^j X_{M,t}^j)\}}_{\text{Reported profits less expensed investments and taxes}} \end{aligned}$$

where  $\chi_i^i = 1$  and  $\chi_i^j = 0, j \neq i$



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given definition of dividends,

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$\Rightarrow$  expensing done at home



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Key result: accounting profits are not equal to true profits